[Problem #1](https://erdos.sdslabs.co/problems/1)

Minimum Value

Let there be a set of *N* natural numbers 1,2,3,4...*N*. We are allowed to insert + or − sign in front of each number and add all the resultant numbers. The minimum non-­negative value obtained is denoted as *D*(*N*).

Find the value of *D*(1)+*D*(2)+...+*D*(19216812112)

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #2](https://erdos.sdslabs.co/problems/2)

Equation

Let *x* and *y* be positive real numbers.

Using the equation *y*6=*x*6+8*x*4−6*x*2+8, find the integral value of 3345*x*+4321*y*2.

Your answer should not exceed 107.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)  [polynomial](https://erdos.sdslabs.co/tags/polynomial)

[Problem #3](https://erdos.sdslabs.co/problems/3)

Largest Number

Find the positive integer *n* less than 100000 for which the equation *x*2=*ny*2+1 has the largest fundamental value of *x*. The fundamental value of (*x*,*y*) is the smallest positive non-trivial integral solution to the equation. (1,0) is the trivial solution.

Note: You can ignore those values of n for which there are no fundamental solution to the given equation.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #4](https://erdos.sdslabs.co/problems/4)

Palindromes

Find the sum of numbers less than or equal to 1000000000 which are palindromes in binary, octal as well as hexadecimal base.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [palindrome](https://erdos.sdslabs.co/tags/palindrome)

[Problem #5](https://erdos.sdslabs.co/problems/5)

3 Musketeers

There are 3 people A, B and C. Three of them have positive integers written on their hats. One can only see the numbers written on others hats and can not see the number written on his own hat. The number on one of the hats is the sum of the numbers on the other 2 hats. Now the following event occurs

* A was asked about the number on his hat. He replies "Don't know".
* B was asked about the number on his hat. He also replies "Don't know".
* C was asked about the number on his hat. He also replies "Don't know".
* A was asked again the number on his hat. He replies "65".

Find the product of the three numbers on the hats.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [implementation](https://erdos.sdslabs.co/tags/implementation)

[Problem #6](https://erdos.sdslabs.co/problems/6)

Sum It Up

Let *A* be the sum of digits of 33343334 when written in decimal notation and *B* be the sum of digits of *A*.

What is the value of 2013 times sum of digits of *B*?

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #7](https://erdos.sdslabs.co/problems/7)

## Exponentiation



You are given that *f*(2,10) mod 1000000007 = 180974681

Calculate 

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #8](https://erdos.sdslabs.co/problems/8)

## Summation of Primes

Find the sum of digits of all prime numbers below 109.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [primes](https://erdos.sdslabs.co/tags/primes)

[Problem #9](https://erdos.sdslabs.co/problems/9)

## Highly Divisible Number

What is the smallest number to have over 300 divisors?

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [divisors](https://erdos.sdslabs.co/tags/divisors)

[Problem #10](https://erdos.sdslabs.co/problems/10)

## Number Spiral Diagonals

Starting with the number 1 and moving to the right in a clockwise direction a 5 x 5 spiral is formed as follows:

21 22 23 24 25  
20 07 08 09 10  
19 06 01 02 11  
18 05 04 03 12  
17 16 15 14 13

It can be verified that the sum of the numbers on the diagonals is 101.

What is the sum of numbers on the diagonals in a 10001 x 10001 spiral formed in the same way?

[path traversal](https://erdos.sdslabs.co/tags/path%20traversal) [matrices](https://erdos.sdslabs.co/tags/matrices)

[Problem #11](https://erdos.sdslabs.co/problems/11)

## Factorial

Find 1000000008!

Give the answer modulo 1000000009.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular) [primes](https://erdos.sdslabs.co/tags/primes)

[Problem #12](https://erdos.sdslabs.co/problems/12)

## Prime Gaps

A prime gap is the difference between two successive prime numbers. The *nth* prime gap is the difference between the (*n*+1)*th* and the nth prime numbers.

Using [**12.txt**](https://erdos.sdslabs.co/files/problems/12.txt), find the largest prime gap for all the primes in the file.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [primes](https://erdos.sdslabs.co/tags/primes)

[Problem #13](https://erdos.sdslabs.co/problems/13)

## Pandigital Primes

A number is said to be pandigital if it contains each of the digits from 0 to 9 (and whose leading digit must be nonzero). Find the smallest pandigital prime number.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [primes](https://erdos.sdslabs.co/tags/primes) [pandigital](https://erdos.sdslabs.co/tags/pandigital)

[Problem #14](https://erdos.sdslabs.co/problems/14)

## Count Fibonacci

Find the number of Fibonacci numbers in the file [**14.txt**](https://erdos.sdslabs.co/files/problems/14.txt).

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [fibonacci](https://erdos.sdslabs.co/tags/fibonacci)

[Problem #15](https://erdos.sdslabs.co/problems/15)

## Blind Fold

In a game, played between 2 players there is a circular field and one of the players is blindfolded, who stands in the center of the field. The other player stands at a fixed point on the circumference of the circular field. On the word **GO**, the blind-folded player starts running towards the edge of the field while the second player's aim is to run in and catch him before he moves out of the circle.

If the blind-folded player runs in a random direction with a constant speed *v* while the second player runs towards the first player with a constant speed *m* times *v*, what should be the value of *m* such that the probability that the second player wins is 0.50?

Report ans as *m*\*106. If answer is not an integer, round it off to the nearest integer.

[probabilities](https://erdos.sdslabs.co/tags/probabilities) [calculus](https://erdos.sdslabs.co/tags/calculus)

[Problem #16](https://erdos.sdslabs.co/problems/16)

## GCD

Find the Greatest Common Divisor of  and .

Since the answer can be very large, enter the answer modulo 1000000007

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [gcd](https://erdos.sdslabs.co/tags/gcd)

[Problem #17](https://erdos.sdslabs.co/problems/17)

## Magical Matrix

Let 0 < *t* < *u* < *v*, where *t*, *u* and *v* are integers. Now, there is a matrix *Q* with three rows and *c* columns where *c* > 1. The matrix is special in a way that each of its columns contains the three numbers *t*, *u* and *v* in some order. All the 3 numbers must appear in every column. Sum of all numbers in row 1 is 20, sum in row 2 is 10 and in row 3, the sum is 9. The rows are numbered 1, 2, 3 while columns are numbered 1,2,...,*c* and each cell in the matrix is denoted by a pair (*i*,*j*), where *i* = row & *j* = column. Now the cell (2,*c*) contains *v*.

Calculate  for the whole matrix.

[matrices](https://erdos.sdslabs.co/tags/matrices)

[Problem #18](https://erdos.sdslabs.co/problems/18)

## Game

Sandeep and Varun are playing a series of games. Each of them contributes Rs 1000 to start. Varun's chance of winning an individual game is 3 times that of Sandeep's. They make an agreement that whoever wins 5 games first can take the entire money with him. After first 3 games, Varun has won 1 game and Sandeep has won 2 games. Now they are bored and do not want to play further.

So they want to divide the money on the basis of the result of first 3 games.

Let *x* be the money Varun gets and *y* be the money Sandeep gets. Find *xy*. If *x* and *y* are not integers, round them to nearest integer. Since answer can be very large, enter the answer modulo 109+7.

[probabilities](https://erdos.sdslabs.co/tags/probabilities) [expectation value](https://erdos.sdslabs.co/tags/expectation%20value)

[Problem #19](https://erdos.sdslabs.co/problems/19)

## Large Exponentiation

Find the smallest natural number *n* for which 201413*n* mod 2097152 = 1.

Since *n* can be very large, enter answer as *n* mod 1000000007.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #20](https://erdos.sdslabs.co/problems/20)

## Fives and Sevens

How many 20-digit numbers are there which are formed using only the digits 5 and 7 and divisible by both 5 and 7.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [divisors](https://erdos.sdslabs.co/tags/divisors) [combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #21](https://erdos.sdslabs.co/problems/21)

## Two Squares

You are given 2 squares such that sum of their area is 1. You want to fit these 2 squares inside a rectangle, without overlap, such that sides of the rectangle are parallel to the sides of the squares. Find the area of smallest such rectangle for which we can always fit the 2 squares as per the given constraints.

Enter answer as 10000000 \* *area*. In case the answer is not an integer, return the answer rounded off to the nearest integer.

[geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #22](https://erdos.sdslabs.co/problems/22)

## Totient Function

Let *X* be the smallest number having *ϕ*(*X*) equal to 108. Find the number of digits in the factorial of *X*.

*ϕ* stands for Euler's Totient Function.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [totient](https://erdos.sdslabs.co/tags/totient)

[Problem #23](https://erdos.sdslabs.co/problems/23)

## Crack The Safe

There is a safe with its 10-digit keypad (as shown below) which is to be cracked.

9 8 7  
6 5 4  
3 2 1  
0

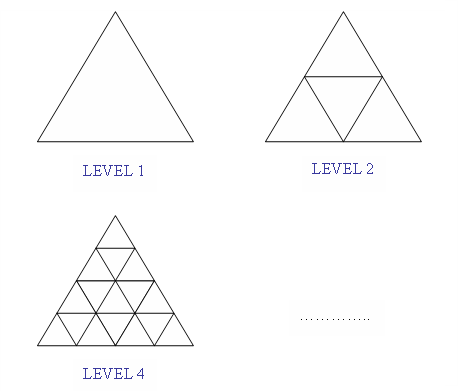
The restriction of the password for that safe is that every pair of neighboring keys in the password is adjacent on the keypad. Adjacent keys are the ones that share a common edge. You know that the password is 109 digits long. Let total number of possible passwords for this safe be *X*. Since *X* can be very large, enter *X* mod 109+7.

[implementation](https://erdos.sdslabs.co/tags/implementation)

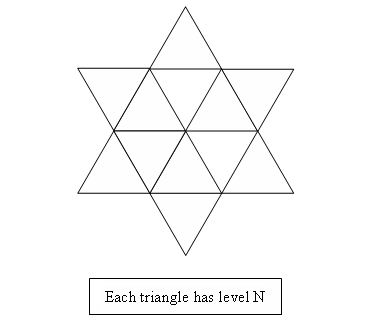
[Problem #24](https://erdos.sdslabs.co/problems/24)

## Tangles

We define the LEVEL of a triangle as in the following image:



Similarly we can define the LEVEL of a hexagram. It's called level n hexagram if it’s joined by 12 triangles, each one is a level n triangle.



Let us define *X*(*n*) as the total number of triangles in a level *n* hexagram. Then *X*(*n*) can be written as a polynomial in terms on *n*.

Let *Y* be the product of non-zero coefficients of polynomial *X*(*n*). Find the factorial of *Y*. Since answer can be very large, enter the answer modulo 109+9

[geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #25](https://erdos.sdslabs.co/problems/25)

## Butter's Prime Floor

Let there be functions *f*(*N*) = no. of primes *x* <= *N* and *g*(*N*) = 

Find the value of  .

[Problem #26](https://erdos.sdslabs.co/problems/26)

## Cartman’s Challenge

How many polynomials are there of degree 59 with leading coefficient 1 which cannot be factored in the field of

4113101149215104800030529537915953170486139623539759933135949994882770404074832568499?

If your answer is *x* then input *x* mod 1000000007

[Problem #27](https://erdos.sdslabs.co/problems/27)

## When Kenny Guesses

Let there be an expression . The task is to approximate the value of *θ* so that it gives prime for values from *n* = 1 to *n* = 12. Give the answer correct upto 14 decimal places

[Problem #28](https://erdos.sdslabs.co/problems/28)

## Mrs Cartman’s Desire

Mrs Cartman likes rotational symmetry (everything which is symmetric about the centre) She had a long cherished desire of playing chess. So Randy Marsh challenges her to solve the following puzzle:

She is asked to arrange the non-attacking rooks on the chessboard according to Mrs Cartman’s fantasies, only if possible. She is given chessboards of different sizes (n∗n) and asked what are the total number of ways of arranging n rooks if n varies from 1 to 61. Give the answer modulo 1000000007.

[Problem #29](https://erdos.sdslabs.co/problems/29)

## Mr. Garrison Prepares for the Night

Suppose that Mr Slave wants to buy *n* sandals *s*1,*s*2,*s*3,*s*4...*sn* and *n* dresses *d*1,*d*2,*d*3,*d*4...*dn*, where *si* is a must to have bought before buying *si*+1 and the same with *di*. Let the ordered ways to add these 2*n* things to the girl's clothing be *a*(*n*), *n* varies from 1 to 60. So calculate



[Problem #30](https://erdos.sdslabs.co/problems/30)

## Respect My Authoritah!

The wizard Cartman decides to color a torus with colors. Let the minimum number of colors required to color the *n*-holed torus be *m*(*n*). He has a cube of iron. He asks the blacksmith token to cut it (as in a laser plane is passing through the cube) *n* times. Let the number of different parts of the cube generated be *x*(*n*). But he loves to work with prime numbers and so wants *x*(*n*)−*k* and *x*(*n*)+*k* to be prime. Let the smallest *k* required to accomplish it be *f*(*n*). Your task is to find out 

[Problem #31](https://erdos.sdslabs.co/problems/31)

## When Butter Sums It Up

The positive real numbers *x*0,*x*1,*x*2...*xm* satisfy *x*0 = *xm* and *xi*−1 + *k*/*xi*−1 = *k* *xi*+ 1/*xi*

Let *x*0(*k*,*m*) be its maximum possible value of *x*0 .

If (*k* = 2 and *m* = 59), find the summation of such *x*0(*k*,*m*) when you increase *k* by 1 and at the same time decrease *m* by 2 till both become equal.

[Problem #32](https://erdos.sdslabs.co/problems/32)

## Japanese Robo Awesome-O

Professor Chaos controls the robot Awesome-O by pressing the forward or back button. He presses the forward button *n* times and the back button *n* times, one at a time. It returns back to him after he presses the buttons 2*n* times.

Let *a*(*n*,*i*) be the number of ways such that the number of moves in the forward direction do not exceed the number of moves in the backward direction and the number of positive moves in the forward direction equals the number of positive moves in backward direction exactly for *i* times.

Given *a*(3,1) = 2, *a*(3,2) = 2 and *a*(3,3) = 1.

Professor Chaos enters an *n*\**n* square board. He can traverse from (0,0) to (*n*,*n*) in all possible ways but is restricted to (1,0), (0,1) and (1,1) directions only. Let *b*(*n*) be the number of steps on line *x* = *y* in all possible paths on which Chaos can travel.

Given *b*(2)=6.

Let 

Find 

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #33](https://erdos.sdslabs.co/problems/33)

## Angriff der Nazis

In the quiet little mountain town of South Park, there is a square wheat farm ABCD (sides parallel to N-S & E-W directions) with A being towards North-West and A-B-C-D being in clockwise order. The town is attacked by Nazi Bombers and 5 bombs are dropped on the field. Each bomb burns the crop in a radius of 12 km. First bomb is dropped at a point O such that AO is 34 km, BO is 40 km and CO is 26 km. Other bombs are dropped 10 km north, 15 km south, 30 km east and 27 km west, respectively of O.

Find the area of unburnt crop in the farm rounded upto 3 decimal places.

[Problem #34](https://erdos.sdslabs.co/problems/34)

## Jewish Factorials

Find in how many ways can we write 100! as a sum of two or more consecutive positive numbers.

Give the answer mod (1000000009)

[Problem #35](https://erdos.sdslabs.co/problems/35)

## Cartman’s Large Growing Sequence

Consider the fraction 

This is a normal fraction which can be written as recurring decimals. Here, the same alphabets stand for the same digits. Find the sum *S* of all such fractions with distinct values of the fraction. *S* = *p*/*q* in its most simplified form. Answer *p*\**q*.

[Problem #36](https://erdos.sdslabs.co/problems/36)

## What’s the Answer Makey?

Mrs. Broflovski, Kyle’s mother asked Mr. Makey, "Kyle was visited by three wizards today. If you multiply their ages, you’ll get 2450, and together their age is 2 less than your age. Can you tell me their ages?" After deep thought, the teacher said "No, I can’t." Then Mrs. Broflovski said, "Of course you can’t, but if I tell you that the oldest wizard is older than Kyle, you should be able to work out."

Give the sum of cubes of ages of the three wizards as well as Kyle.

[Problem #37](https://erdos.sdslabs.co/problems/37)

## The Allowance Problem

Stan gets his allowance on the 15th day of every month, he gets 1 dollar if its a Monday, 2 dollars if it’s a Tuesday, 3 dollars if its a Wednesday and so on ... 7 dollars if it’s a Sunday. Then on a particular 15th of a random month, find the expected value *e* of the money Stan will be receiving. Give the integer after ignoring decimal in *e*\*1000000.

[Problem #38](https://erdos.sdslabs.co/problems/38)

## When Mr. Garrison Teaches Geometry

A hexagon with area *A* and consecutive sides of lengths 8, 10, 8, 10, 12 and 12 is inscribed in a circle. Let *N* = 100\**A*, ignoring the decimal part which may be represented as *xk*\**y*, where *x*,*y*,*k* > 1. Take *Y* as the average of all possible *y*s in the above expression and find the *Y*th prime number.

[geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #39](https://erdos.sdslabs.co/problems/39)

## XOR 'em Up

Say *f*(*n*) = bitwise XOR of all natural numbers up to a positive integer *n*.

Find *f*(22013) mod 1000000007.

[Problem #40](https://erdos.sdslabs.co/problems/40)

## Kyle's Mysterious Sequences

For a given integer *n*, Consider the following functions *G*(*n*) and *F*(*n*)



Now consider the sequences



Find the value of 

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #41](https://erdos.sdslabs.co/problems/41)

## Cartman Loves One Direction

Find the number of occurrences of the digit 1 in all natural numbers between 123456789 to 1234567890.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #42](https://erdos.sdslabs.co/problems/42)

## Medical Marijuana

Men in South Park are suffering from vulva cancer and are getting doctor's reference for medical marijuana. The demand for the same has gone up. A transport company handling the shipments has *n* identical articles which are to be shipped in k identical trucks.

You simply have to find the total number of ways of distribution of those articles in the trucks.

Compute for *n* = *k* = 10000.

Answer mod 1000000007.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [integer partition](https://erdos.sdslabs.co/tags/integer%20partition) [dp](https://erdos.sdslabs.co/tags/dp)

[Problem #43](https://erdos.sdslabs.co/problems/43)

## Game of Stacks

Drake and Josh play a game to take a break from programming. In this game, there is a stack of *N* sheets. Drake starts first and alternating turns, they remove an odd number of sheets in each turn and put them in a basket which is initially empty. After every turn they note down the count of the sheets in the basket and thus construct an increasing sequence of numbers. But then, Drake wonders, how many distinct games of this kind can they play such that the stack gets empty at last and there are exactly *k* numbers in the sequence i.e. the game ends after *k* turns. Josh answers this when *N* and *k* were small. But now Drake who is also good in Mathematics asks you the same question with slight complications:

*N* = 999999 and *k* = 5*p* can be any number where  is a perfect square, i.e. you have to take the sum for all such *k*!

Give your answer mod 109+7.

Note that distinct games generate distinct sequences.

[Problem #44](https://erdos.sdslabs.co/problems/44)

## Power Sum

Let *k* = 41286 + 64128.

What is  (units digit of kn+nk)?

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #45](https://erdos.sdslabs.co/problems/45)

## One of Us

Let *a*(*n*) be defined as the number of terms in the sequence 21,22,...2*n* which begin with digit 1.

Find 

Give your answer as the largest integer after multiplying by 106.

[calculus](https://erdos.sdslabs.co/tags/calculus)

[Problem #46](https://erdos.sdslabs.co/problems/46)

## When Butter Recurses

Let us define a series *M* such that *M*(*n*−1) + *M*(*n*+1) = 5\**F*(n) where *F*(n) is the *n*th term of the Fibonacci sequence with *F*(0) = 0, *F*(1) = 1 and *M*(0) = 2.

Find the value of

Give answer mod1000000007

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [fibonacci](https://erdos.sdslabs.co/tags/fibonacci)

[Problem #47](https://erdos.sdslabs.co/problems/47)

## Stan’s Prime Challenge

What is the number of primes of the form 4*k* + 3 between 8589934592 and 17179869184?

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [primes](https://erdos.sdslabs.co/tags/primes)

[Problem #48](https://erdos.sdslabs.co/problems/48)

## Mr Garrison Can't Get a Period

Consider *F*(*n*) as the last 8 digits of the *n*th Fibonacci number.

What is the period of *F*(*n*)?

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [fibonacci](https://erdos.sdslabs.co/tags/fibonacci)

[Problem #49](https://erdos.sdslabs.co/problems/49)

## Hyper Sum of Fibonacci Numbers

Let *F*(*n*) be the *n*-th Fibonacci number. That is, *F*(*n*) satisfies

*F*(0) = 0, *F*(1) = 1, *F*(*n*) = *F*(*n*−1) + *F*(*n*−2)  (if *n* ≥ 2).

Let *fk*(*n*) be the function such that





You are given that *f*1(1) = 1, *f*2(2) = 3 and *f*10(10) = 130965.

Find *f*108(108) (mod 1 000 000 007).

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [fibonacci](https://erdos.sdslabs.co/tags/fibonacci) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #50](https://erdos.sdslabs.co/problems/50)

## Divisibility

Find the base of a counting system, like decimal(10), binary(2) etc., less than 1000000 in which maximum numbers follow the following property:

"If *x* is divisible by *y*, sum of digits in *x* will also be divisible by *y*."

In case there is more than 1 possible answer, then concatenate the possible answers in ascending order without any spaces in between. For example if the answers are 3, 21 and 54 then your answer should be 32154.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #51](https://erdos.sdslabs.co/problems/51)

## Probability of Squares

Two numbers are chosen at random from 1 to 1016. Let *p* be the probability that their sum is a perfect square. Find integral part of 1016\**p*.

[probabilities](https://erdos.sdslabs.co/tags/probabilities)

[Problem #52](https://erdos.sdslabs.co/problems/52)

## Modular Roots

Let *y* = *x*\**x*. \* is multiply modulo *N* = 4776913109852041418248056622882488319.

You have to find the smallest positive *x* for *y* = 739397.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #53](https://erdos.sdslabs.co/problems/53)

## Harry and his Magical Boxes

There are 7 magical boxes each containing a label depicting a number. The labels of the boxes are given as 5,2,7,8,7,4,6. Harry Potter goes to each jar once and shouts a spell. When Harry shouts a spell near a box with label *x* he gets a random integer n from the box such that, 1 <= *n* <= *x*. Thus he gets a collection of seven numbers by shouting once near each box. One such collection is 4,2,1,2,6,4,6. Two collections are same if one is a permutation of other. So 1,2,1,1,1,1,6 is same as 2,1,1,1,1,1,6. Now Harry expects you to tell the total number of different collections he can get by repeatedly performing this act.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #54](https://erdos.sdslabs.co/problems/54)

## Find Tuples

Let *S* denote the set of all 6-tuples (*X*1,*X*2,*X*3,*X*4,*X*5,*X*6) of positive integers such that 

Consider the set .

Find the HCF of all members of *T*.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [gcd](https://erdos.sdslabs.co/tags/gcd)

[Problem #55](https://erdos.sdslabs.co/problems/55)

## Double Devils

All numbers of the form **6\_6\_6\_0\_0\_6\_6\_6\_0\_0**, where each **\_** can be any single digit, are called double devil numbers (for example, 6160630507696864040 is a double devil number).

Let *x* be the unique number whose square is a double devil number. Find *x*.

[Problem #56](https://erdos.sdslabs.co/problems/56)

## Playing with Subgraphs

Find the number of distinct sub-graphs of a complete graph of *n* labelled vertices, such that the sub-graph is a spanning tree connecting all the vertices and the degree of no vertex is more than 3.

Given *n* equals 314159, give your answer (mod 1 000 000 007).

[Problem #57](https://erdos.sdslabs.co/problems/57)

## Smallest Perimeter

The sides of a triangle have integer lengths *k*, *m* and *n*.

Assume that *k* > *m* > *n* and.

where {x} denotes the fractional part of a number.

Determine the minimum value of the perimeter of the triangle.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #58](https://erdos.sdslabs.co/problems/58)

## Circle of Death

Let *n* be 10 times the largest integer which cannot be represented as the sum of five non-zero perfect squares. Now, consider yourself standing in a circle of n people (positioned 1 to *n* around the circle), where every *k*th (*k* = 10) person is killed from the remaining ones standing except the last one. For example, if *n* = 4 and *k* = 2, then the order in which people will be killed is 2, 4, 3. Hence person at position 1 will be the survivor.

Let *p* be the position you will choose so as to survive this game (be the last to be killed). Also, for *n* = 40, let *q* be the smallest value of *k*(>1) for which people are killed in the same order as they are standing (i.e. 1,2,3,...).

What is (*p*\**q*) mod 1000000009?

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [dp](https://erdos.sdslabs.co/tags/dp)

[Problem #59](https://erdos.sdslabs.co/problems/59)

## Ones and Zeros

Let *S* = 2*a*+2*b*+2*c*+2*d*+2*e* where *a*,*b*,*c*,*d*,*e* are distinct whole numbers.

Let *Sn* be the *n*th number such that for all *i* < *n*, *Si* < *Sn* and for *i* > *n*, *Si* > *S*.

Find *S*2131646 mod 109+7.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #60](https://erdos.sdslabs.co/problems/60)

## Rolling Dice

Alex has a 7-sided regular dice. Every side has a distinct value between 1 to 7, each with equal probability of coming up in a roll. Alex rolls the dice once. Let the value obtained be equal to *S*1. Now he rolls the dice *S*1 number of times. Let the sum of values obtained in these *S*1 rolls be equal to *S*2. Now he rolls the dice *S*2 number of times. Let the sum of the values obtained in these *S*2 dice rolls be equal to *S*3. This process is continued for an infinite number of times. Find the expected value of *S*1182014. If the answer is *x*, give your answer as  mod 109+7, where  denotes the greatest integer less than or equal to *x*.

[Problem #61](https://erdos.sdslabs.co/problems/61)

## Derangements

There are *n* people and *n* houses, such that every person owns exactly one distinct house. Out of these *n* people, *k* people are special (*k* <= *n*). You have to send every person to exactly one house such that no house has more than one person, and no special person goes to his own house. Let *S*(*n*,*k*) be the number of ways of doing this. Find the value of *S*(654321,123456). Give your answer mod 109+7.

[Problem #62](https://erdos.sdslabs.co/problems/62)

## Magic in Boxland

A magician lives in a mysterious Boxland that comprises of eight cities and all of them contain 6 magic wands. Each wand has been colored with one of *n* colors, such that no two wands in the same cities are of same color, and no two colors occur together in more than one city. The smallest number *n* that satisfies this condition is used by the magician to create a ball-box challenge that contains a 2-D array of size *n*\**n* of such boxes placed adjacent to each other satisfying following conditions:

* Every box that does not contain a ball shares a side with one which does.
* Given any pair of boxes that contain balls, there is a sequence of boxes containing balls, starting and ending with the given boxes, such that every two consecutive boxes of the sequence share a side.

Find the smallest number of balls that must be there inside those boxes multiplied by 3.

(i.e. Answer = [Total number of balls inside the array of boxes] x 3)

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics) [graphs](https://erdos.sdslabs.co/tags/graphs) [greedy](https://erdos.sdslabs.co/tags/greedy)

[Problem #63](https://erdos.sdslabs.co/problems/63)

## Seat Yourself

Let *x* be the number of students seated around a round table. Then, let *k* be the number of ways in which they change their seats resulting in an arrangement in which the students are either on the same seat or one of the seats adjacent to the original one.

Given that *x* belongs to the set (123345857, 343139869), both not-included, find the possible number of values of *k* which are congruent to 111 mod 5.

[Problem #64](https://erdos.sdslabs.co/problems/64)

## Polynomials

Consider a polynomial of degree 3*m* such that

*P*(0) = *P*(3) = *P*(6)...*P*(3*m*) = 2

*P*(1) = *P*(4) = *P*(7)...*P*(3*m*−2) = 1

*P*(2) = *P*(5) = *P*(8)...*P*(3*m*−1) = 0

and *P*(3*m*+1) = 6562

Find the value of *m*?

[Problem #65](https://erdos.sdslabs.co/problems/65)

## Identical Boxes

You are given 2500 identical boxes and 5000 identical balls. Find the number of ways in which balls can be distributed such that each box contains at least one ball. Assume the capacity of each box to be infinite.

Give your answer mod109+7.

Note: All permutations of boxes are counted as a single way as the boxes are identical.

[Problem #66](https://erdos.sdslabs.co/problems/66)

## Reaching Point

You have to reach point (*x*2,*y*2) from (*x*1,*y*1) by making jumps from one point to another but you have some limitations. You can only move in the direction of the line connecting these two points constantly aiming towards the destination point. Also from one point you can jump to only the next most nearest integral point on the line. For example, (3,3) to (6,6) then path has to be (3,3)−>(4,4)−>(5,5)−>(6,6) and this required 3 jumps. But now the problem is the a jump comes at a heavy cost.

If the total number of jumps made to reach (*x*2,*y*2) starting from (*x*1,*y*1) is n, then the total cost for the journey is said to be the (number of trailing zeroes in *n*!)*n*.

Find the total cost for the journey from (−10101099, 127898755387) to (1137947000140424, 1607032990556) mod 109+7.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #67](https://erdos.sdslabs.co/problems/67)

## Finding Limits



Find *Sx* mod 1073741824 where *x* tends to infinity.

[Problem #68](https://erdos.sdslabs.co/problems/68)

## A Mixture of Ryski's Problems

Ryski was asked compute the sum of the series



Let this summation be *p*.

Ryski also has 2\**n* different pens (*n* ∈ *N*, *n* ≥ 2). Each day, he takes *n* pens with him to school. After some days the following condition was fulfilled: every two pens were together on at least one day. Let the minimum number of days needed for this to happen be *q*.

Give the answer as [*p* \* *q* \* 1020], where [*x*] denotes the greatest integer less than or equal to *x*.

[Problem #69](https://erdos.sdslabs.co/problems/69)

## Trio Interchange

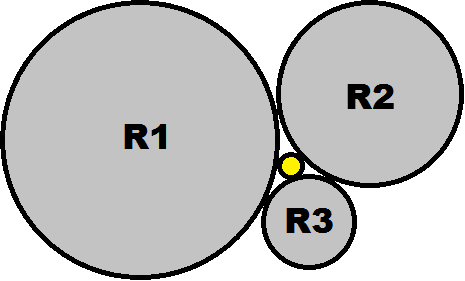
There is a six digit number, which when multiplied with 6, yields another six digit number, with first three digits of original number as the last three digits of the new number, in the same order, and the last three digits of the original number as the first three digits of the new number, in the same order.

Let *S* be the sum of the digits of that number. Find *S*! mod 1000000007

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #70](https://erdos.sdslabs.co/problems/70)

## Fibonacci Circle



All circles in the picture above are tangent to each other. If radius *R*1 = 212, *R*2 = 211 and *R*3 = 210, calculate *r*, radius of the inner yellow circle. Let .

We now define a new sequence as

*F*(*n*) = *F*(*n*−1) + *F*(*n*−2) + (*n*−1) ∀ *n* ≥ 2

with *F*(0) = 0 & *F*(1) = 1.

Calculate sum {*F*(0)+*F*(1)+*F*(2)+...+*F*(*x*−1)+*F*(*x*)} mod 1000000007.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #71](https://erdos.sdslabs.co/problems/71)

## Random Selector

A random number selector can only select one of the nine integers 1,2,...,9, and it makes these selections with equal probability. Let p be the probability that after n selections (*n* > 1), the product of the *n* numbers selected will be divisible by 10. If *n* = 5, find *p* × 59049.

[probabilities](https://erdos.sdslabs.co/tags/probabilities)

[Problem #72](https://erdos.sdslabs.co/problems/72)

## GitHub

You are given six characters GITHUB to make a string of length *N*. However there are some limitations:

* I can not come directly after G.
* H can not come directly after G or B.
* T can not come directly after T or U.
* The string should be a palindrome.

How many ways are there to form a string of length *N* = 7162534?

Submit the answer modulo 1000000007.

[dp](https://erdos.sdslabs.co/tags/dp)

[Problem #73](https://erdos.sdslabs.co/problems/73)

## Brute

*x*6 + *x*3 + *x*3*y* + *y* = 147157

*x*3 + *x*3*y* + *y*2 + *y* + *z*9 = 157147

Let n be the number of solutions for the above system. i.e. if *x* = *a*, *y* = *b*, *z* = *c* is a solution then the number of solutions is incremented by 1. Give your answer as first six digits of (*n* + e)134.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #74](https://erdos.sdslabs.co/problems/74)

## Mod It

Let *n* be the largest positive integer, such that *n*! can be expressed as the product of (*n*−20142015) consecutive integers.

Let *x* be equal to *n* mod 38980715857. Find *x* mod 8037517.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #75](https://erdos.sdslabs.co/problems/75)

## No Primes

Find sum of all 5-digit natural numbers such that they don't contain any subsequence forming prime number. 2, 3, 4 or even 5-digit prime numbers are not allowed.

[brute force](https://erdos.sdslabs.co/tags/brute%20force)

[Problem #76](https://erdos.sdslabs.co/problems/76)

## Erdős

Given that *e*,*r*,*d*,*o*,*s* are real numbers such that

*e* + *r* + *d* + *o* + *s* = 8

*e*2 + *r*2 + *d*2 + *o*2 + *s*2 = 16.

Let *M* be the maximum value of *s*. Find the number of factors of *M*×30.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #77](https://erdos.sdslabs.co/problems/77)

## Prime Fangs

In mathematics, a vampire number is a composite natural number *v*, with an even number of digits *n*, that can be factored into two integers *x* and *y* each with *n*/2 digits and not both with trailing zeroes, where *v* contains precisely all the digits from *x* and from *y*, in any order, counting multiplicity. *x* and *y* are called the fangs, e.g. 1260 = 21 × 60.

A prime vampire number is a vampire number whose fangs are its prime factors. 117067 = 167 × 701 is the first prime vampire number. Calculate the 27th prime vampire number.

[brute force](https://erdos.sdslabs.co/tags/brute%20force)

[Problem #78](https://erdos.sdslabs.co/problems/78)

## Golden Path

Let *x* be a number such that for *n* > *x*, the nth Fibonacci number has at least one prime divisor that does not divide any *k*th Fibonacci number for all *k* < *n*. Find the sum of all primes *p* < 10*x* such that for some integer n, the expression *n*2−*p*×*n* is a prime power.

Note: A prime power is a number of the form *qm* where *q* is a prime and *m* is a positive integer.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #79](https://erdos.sdslabs.co/problems/79)

## Strings

Laertes and Roxane play a game together by first drawing a string of *L*s and *R*s into the sand, and then taking turns removing any one of their respective letters (*L* for Laertes and *R* for Roxane) along with the substring to its right. The first player unable to make a move loses the game.

Consider the game played with the string *L*. If Laertes goes first, he removes the only *L* and passes to Roxane, who immediately loses, having no valid move. If Roxane goes first, she immediately loses again. So we see that Laertes always has at least one move's worth of an advantage over Roxane. We shall abbreviate this by saying the value of the string *L* is +1, from Laertes' point of view. Similarly, the string *R* has value −1. A game played with the two separate strings, *L* and *R* (denoted by *L*+*R*) can be shown to have the property that the first player to play loses the game. We shall call the value of such a string 0, and denote this as *L*+*R*=0.

Convince yourselves that *LR*=0.5 (try playing the game with *LR*+*LR*+*R*). What is the value of *LRL*?

[strings](https://erdos.sdslabs.co/tags/strings)

[Problem #80](https://erdos.sdslabs.co/problems/80)

## Piles of Stones

Laertes and Roxane play another game now as they are tired of drawing in the sand. Instead, they play a game with piles of stones that works as follows:

At the beginning of each turn, the player first chooses one of the piles and then removes some number of stones from it (the whole pile may be removed as well, but at least one stone needs to be removed). The turn then passes to the next player. The player that removes the last stone(s) wins.

Laertes always goes first.

Convince yourself that in a game with three piles of 3, 4, and 5 stones respectively, Laertes will always win if he plays optimally, no matter what Roxane does. Let's say that games with this property have value 1.

Consider 6561 separate games, with four piles, and the number of stones per pile varies between 1 and 9. How many of these games have value 1?

[games](https://erdos.sdslabs.co/tags/games)

[Problem #81](https://erdos.sdslabs.co/problems/81)

## Hide and Seek

Laertes and Roxane go to the Senate to play a game of Hide-and-Seek. There are 100 rooms in the Senate, and Roxane picks one of them and hides there till the game ends.

Laertes, at the beginning of every turn, picks one room and searches in it. Since he is human and thus fallible, he only has a 60% chance of finding Roxane if she is in fact hiding in the room. If he fails to find her in the room, Roxane's score increases by one, and the next turn starts, whereupon Laertes must pick another room to check (he can also check the same room again). Remember, Roxane remains in the room she initially chose.

Given that Laertes and Roxane play with perfect strategies, what is the expected value of Roxane's score at the end of the game? The answer must be correct to 1 place of decimal.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #82](https://erdos.sdslabs.co/problems/82)

## Pebble Trouble

Laertes and Roxane play a game with some black and white pebbles at the beach. They dig twelve small pits in the sand, making a dodecagon. Laertes will place two stones, one black and one white into two adjacent pits in such a way that the white stone is to the left of the black. Laertes cannot then place any stones in the pits next to these. Similarly, Roxane places her stones so that the white one is to the right of the black one. She too cannot use the adjacent pits ever again.

The first person who is unable to place their pair of stones loses. If Laertes goes first, convince yourselves that Roxane can always win with perfect play.

Consider 1000 games where the number of pits in the sand varies from 12 to 1011. How many of these games can Roxane always win, if Laertes goes first each time?

[games](https://erdos.sdslabs.co/tags/games)

[Problem #83](https://erdos.sdslabs.co/problems/83)

## Fresh from the Oven

Laertes and Roxane have before them a cake, freshly baked by their mother. It has been lightly scored so as to allow it, when cut, to be divided into *M*×*N* pieces. The two kids decide to play a game to cut the cake. Laertes will cut any rectangle into two pieces along the vertical lines, and Roxane along the horizontal lines. The game ends when the first who is unable to make a move loses.

Laertes always goes first.

Consider 256 games with cakes varying in size from 1×1 to 16×16. How many of these games can Laertes always win, if he plays with perfect strategy?

[games](https://erdos.sdslabs.co/tags/games)

[Problem #84](https://erdos.sdslabs.co/problems/84)

## The Gobbler

Laertes and Roxane are tired of cutting cakes. They want to eat some now, and they do so by playing a game as follows:

On his turn, Laertes must choose any square on the grid and eat it, along with the square immediately below it. On her turn, Roxane must choose any square on the grid and eat it, along with the square to its immediate right. The first person who cannot eat two pieces as described above on any turn loses. Let us describe the squares using the conventional matrix coordinate scheme, with the top-left square being (0,0) and the positive x and y axes extend to the right and down respectively. In cases where taking two different squares results in the same cake upto symmetry, then the square that is closest to the origin is preferred. If the square is still ambiguous, then the one that is closer to the x axis is preferred.

Consider the 2×1 cake. It is obvious that no matter who goes first, Laertes can always win by eating the square at (0,0) (and so consequently (1,0)).

The 2×2 cake is different though. Convince yourself that the first person to start will win, no matter who it is.

What are the optimal squares chosen by both players on a 4×2 cake? Assume that Laertes goes first. If you think the sequence is (*a*,*b*), (*c*,*d*), (*e*,*f*), enter *abcdef*.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #85](https://erdos.sdslabs.co/problems/85)

## The Stymphalean Birds

**The story**

The Stymphalean birds were monsters. They were man-eating birds with beaks of bronze and sharp metallic feathers they could launch at their victims. They had destroyed the local crops and fruit trees before Hercules was tasked with killing them. Athena gave Hercules a rattle that he could use to scare the birds off so he could then shoot them down with his bow.

**The game**

It turns out that shaking the rattle in a specific way would induce absolute terror in the birds. Let *L* represent shaking the rattle to the left, and *R* to the right. Then, using the game introduced in [**Problem 79**](https://erdos.sdslabs.co/problems/79), enter the string that has the value 4.740234375.

[strings](https://erdos.sdslabs.co/tags/strings)

[Problem #86](https://erdos.sdslabs.co/problems/86)

## The Augean Stables

**The story**

Hercules' task this time is to clean the Augean stables. They are in a right old mess. Hercules eventually hits upon the idea of diverting a nearby river into the stables in order to clean it. This gets rid of the muck but sadly a lot of vegetation has overgrown on the grounds that Hercules will have to weed out the hard way. In order to pass his time, he invites the local farmhand to play a game with him, using the weeds.

**The game**

Each weed is divided into a certain number of parts, and players take turns cutting off a part. Any section of the plant that is not connected to the ground after a cut is also removed. Play continues until the last person to make a cut wins.

Hercules always goes first.

Each weed is represented as a graph, with edges representing pieces of the plant that can be cut off in a turn. The node labelled 0 is the one that is connected to the ground.

Now, [**here**](https://erdos.sdslabs.co/files/problems/86.txt) are the adjacency matrices of 7 such weeds. Consider the 127 games that can be played with some combination of these weeds. For example, Hercules can always win the game played on just weed 1, but he will always lose the game played with both weeds 1 and 3. Find all the combinations of weeds such that Hercules will always lose the game played with them. Enter your input in the following fashion:

The combination (1,3) is considered as the binary number 1010000 (the first and third places are set to 1), and the combination (1,6,7) is 1000011. Convert your combinations into binary numbers and enter their sum in decimal.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #87](https://erdos.sdslabs.co/problems/87)

## The Flock of Geryon

**The story**

Hercules just got another task. This time he has to steal Geryon’s golden cow from the far-off Mediterranean island of Erytheia. Hercules knows that Geryon has a large flock of cows among which there is only one golden cow, which Hercules needs to retrieve.

Hercules is tired of fighting and challenges Geryon to a bloodless battle instead. The game Hercules suggests is to be played with the remaining cows.

**The game**

Each player chooses to eliminate 13 or 50 or 63 cows from the flock at each turn. The player who eliminates the last set of cows gets the golden cow.

Geryon is not very good at games, so he does not tell Hercules how many cows are there in his flock, lest he thinks of a winning strategy, however in his foolishness he lets slip that the number lies anywhere between 0 to 205530. He also forces Hercules to decide who shall begin the game.

Hercules now wants to know what the odds are of him losing the game if he goes first and plays perfectly, given that the number of cows lies anywhere between 0 and 205530.

Can you help Hercules by finding the probability? The answer must be correct to 4 decimal places.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #88](https://erdos.sdslabs.co/problems/88)

## The Cretan Bull

**The story**

Animals seem to wreak a lot of havoc in greek myths. The one under consideration is a bull that used to uproot crops and bring down orchard walls in Crete. Hercules is sent to kill it as usual.

**The game**

The bull is smart however, and it senses that Hercules is after it. It engages in an impromptu game of hide-and-seek (following the same rules as those in [**Problem 81**](https://erdos.sdslabs.co/problems/81)).

Alas, it only has two choices of hiding places. In the first location, Hercules has a 40% chance to find the bull, if in fact the bull is there. In the second location, Hercules has a 100% chance to find the bull if it is there. The second location is thus a terrible hiding place. But, the bull bets on Hercules dismissing such a location.

If Hercules and the bull play with perfect strategies, what is the expected number of turns it will take for Hercules to capture the bull? The answer is a rational number in lowest terms *p*/*q*, and you are to enter *p*,*q*.

[probabilities](https://erdos.sdslabs.co/tags/probabilities)

[Problem #89](https://erdos.sdslabs.co/problems/89)

## The Horses of Diomedes

**The game**

Hercules and Abderus play a game with a cake (as described in [**Problem 84**](https://erdos.sdslabs.co/problems/84) of the preliminaries). Hercules eats squares horizontally and Abderus vertically. We define the value of a game as:

+1 if Hercules can win no matter who starts,   
−1 if Abderus can win no matter who starts,   
+i if the first player can always win, and   
−i if the second player can always win.

Consider 30 games, played with cakes of sizes *M* × *N*, with 1 ≤ *M* ≤ 3, and 1 ≤ *N* ≤ 10.

What is the sum of the values of these games? If your answer is *a*+i*b*, enter *a*,*b*.

**The story**

Oh, why is Abderus important? He was eaten alive by the crazed horses of Diomedes, and in revenge Hercules fed Diomedes to his own horses. This seemed to have calmed the crazed horses and they lived happily ever after in a meadow somewhere. Greek myths can be very weird sometimes.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #90](https://erdos.sdslabs.co/problems/90)

## Capture of Cerberus

**The story**

Hercules now has to bring back Cerberus, the three headed dog from the underworld. Cerberus being an intelligent beast, lures Hercules to a game of gates. If Hercules wins, he will come back with him, otherwise, Hercules has to spend the rest of his days in the underworld.

**The game**

Rules:

* There are a total of *N* = 18 gates, some of which are open and some which are closed.
* At each turn, the player has to open a closed gate first, and choose to close/open upto 4 gates to the left of the first chosen gate. (Here total number of changed gates *c* = 5). He can either open a closed gate or close an open one.

The player to open the last closed gate wins the game.

**The trial match**

Hercules requests for a trial match and Cerberus agrees to play a toned down version of the above game, with *N* = 5 and *c* = 3. He sets up the initial configuration as this:

CCCCO (C = closed, O = open)

Cerberus urges Hercules to go first. Now, no matter what Hercules does, it is easy to see that Cerberus will always be the one to open the last closed gate. Such a position will always cause Hercules to lose, that is, if he goes first.

Hercules is wary of losing, and wants to make a list of all initial positions where he will lose if he goes first. How many such configurations are there?

[games](https://erdos.sdslabs.co/tags/games)

[Problem #91](https://erdos.sdslabs.co/problems/91)

## The Girdle of Hippolyta

**The story**

Ares had once gifted Hippolyta, the queen of the amazons, a girdle -- a belt. It is this belt that Hercules is now tasked to steal. But, when word of his task spread to the queen herself, she was very impressed with Hercules’ bravery and offered to give him the belt if he won a game of skill against her.

**The game**

Let  be a series for each *i*, 0 ≤ *i* ≤ 7.

And consider  for each *si*.

As an example, let’s play the game with i = 0. Here, , but. Each *In* is of the form *p*/*q* π. We say the value of *s*0 is 8+*p*+*q* (8 being the first integral to break the pattern).

Play the game with all the indicated values of *i*. Add together the values of each *si* and submit this sum modulo 1000000007 as the answer.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #92](https://erdos.sdslabs.co/problems/92)

## The Apples of the Hesperides

**The story**

Hercules has to steal a hundred apples from the Garden of Hesperides. The apple trees are located at a radius of  from the centre (0,0), abundantly distributed (read: infinite amounts) along the circumference.

There is a pole at the centre behind which Hercules is hiding from Ladon, the Dragon lord guarding these trees. Hercules can escape from Ladon only if he is hidden from Ladon's line of sight behind the central pole. Ladon is powerful because he can see in all directions. If Ladon sees Hercules at any point of time, he will immediately fly and kill Hercules.

**Cutting to the chase**

Ladon is travelling to the nearby city of Egypt along a straight line starting from (0,-80), parallel to the x-axis, at a speed of 10 m/s starting at time t=0, nevertheless his all-seeing eye does not tire out from the constant vigilance. Hercules is hiding behind the pole at (0,0) at t=0. Hercules strategizes to pick up the apples located at the circumference, all the while remaining hidden from Ladon's sight, and place them at the centre. But, he can carry only a maximum of 10 apples at a time. Clearly he needs to make 10 such trips. He has a speed of 9 m/s.

What is the shortest time Hercules will need to complete his task, (without getting killed midway, obviously)? If *x* seconds is your answer, enter.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #93](https://erdos.sdslabs.co/problems/93)

## The Ceryneian Hind

**The story**

Hercules’ next task is to catch the Ceryneian Hind, which is as fast as the wind. Artemis considers this a sacred animal and will not give it up to Hercules easily. In order to capture it, he must play a game against Artemis. Artemis has carefully assembled a stick figure of her favourite animal for the game.

**The game**

The figure is made out of sticks which can be either yellow, golden, brown or green. The black line in the figure represents the ground.

At each turn, a player plucks out a stick from the figure. Any "hanging" sticks, i.e. those that have no connection to the ground, either directly, or through other sticks, will fall down and are immediately discarded.

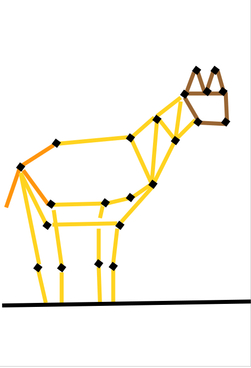
Hercules can only pluck the orange sticks, and Artemis, the brown ones. Both of them can pluck the yellow and green sticks. The one to pluck the last stick wins the game, and gets the Hind.

Hercules also spots a number of other interesting creatures and gambles against Artemis to capture them all, playing the same game for each of them.

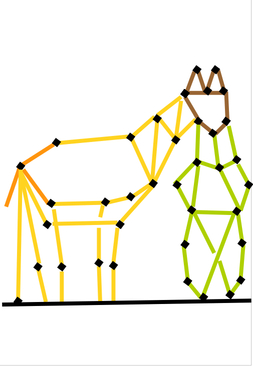
For each game,   
**A** represents Hercules losing no matter who starts, if Artemis plays intelligently.   
**H** represents Hercules wins no matter who starts, if he plays intelligently.   
**F** represents the situation where the first player always loses.   
**S** represents the situation where the second player always loses.

For the 5 figures given below, enter the string of answers in the order of the labels of these figures.

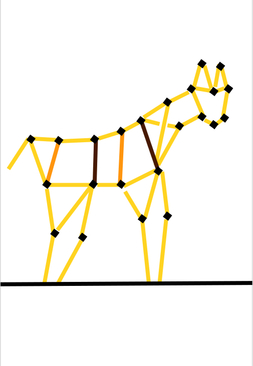
**Golden Hind**



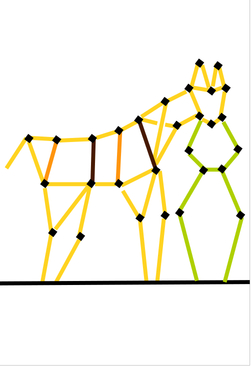
**Golden Hind eating grass**



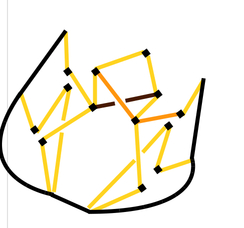
**Wild Zebra**



**Wild Zebra eating grass**



**Poisonous Toad**



[games](https://erdos.sdslabs.co/tags/games)

[Problem #94](https://erdos.sdslabs.co/problems/94)

## Vacation

Ram and Shyam took a vacation at their grandparents' house. During the vacation, they did all activities together. They either played tennis in the evening or practiced Yoga in the morning, ensuring that they did not undertake both the activities on any single day. There were some days when they did nothing. Out of the days that they stayed at their grandparents' house, they were involved in one of the two activities on 22 days. However, their grandmother while sending an end of vacation report to their parents stated that they did not do anything on 24 mornings and they did nothing on 12 evenings. How long was their vacation?

Give your answer in days.

[implementation](https://erdos.sdslabs.co/tags/implementation)

[Problem #95](https://erdos.sdslabs.co/problems/95)

## Strange Currency

In the strange country Oz, the only official coins are 7-cent coins and 13-cent coins. What is the largest amount that cannot be paid with these coins if a shop has no change at all?

[modular](https://erdos.sdslabs.co/tags/modular) [brute force](https://erdos.sdslabs.co/tags/brute%20force)

[Problem #96](https://erdos.sdslabs.co/problems/96)

## The Game of Marbles

A box contains two marbles. One black and the other white. In each turn the player takes a marble out at random and notes its colour. After each turn, the marble is replaced in the bag and an extra black marble is added. The player pays Rs. 1 to play and wins if he/she has taken more white marbles than black marbles at the end.

If the game is played for three turns, the probability of the player winning is exactly 7/24, and so the maximum prize fund that should be allocated for winning in this game should be Rs. 3 before the organizer would expect to incur a loss. The maximum prize is a whole number and includes the Rs. 1 to be given by the player, so the player gets Rs. 2. Find the maximum prize fund to be allocated to a game with sixteen turns.

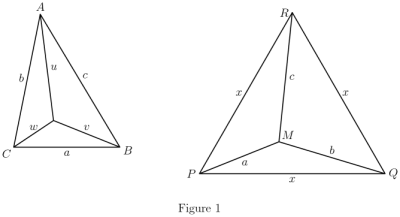
[probability](https://erdos.sdslabs.co/tags/probability)

[Problem #97](https://erdos.sdslabs.co/problems/97)

## Triangles

Let us take two triangles △*ABC* and △*PQR* as shown in Figure 1.

In △*ABC*, ∠*ADB* = ∠*BDC* = ∠*CDA* = 120°.



*u* = 999, *v* = 899, *w* = 1099.

*D* is the internal vertex of △*ABC*

Find the value of *x*.

[geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #98](https://erdos.sdslabs.co/problems/98)

## Series Dilemma

If *Xn* and *Yn* denote two sequences of integers defined as follows:

*X*0 = 1  
*X*1 = 1  
*Xn*+1 = *Xn* + 2×*Xn*−1

*Y*0 = 1  
*Y*1 = 7  
*Yn* + 1 = 2×*Yn* + 3×*Yn* − 1

*n* = 1,2,3,...

Thus, the first few terms of the sequences are:

*X* : 1,1,3,5,11,21,...   
*Y* : 1,7,17,55,161,487,...

Let the largest number that occurs in both the sequences be *m*.

Give the answer as (*m*×123*m*+1)

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #99](https://erdos.sdslabs.co/problems/99)

## Divisibility Test

Sum of digits of a 5-digit number is 41. Let the probability that such a number is divisible by 11 be *p*/*q*, where gcd(*p*,*q*) = 1.

Find *q*−*p*.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [probability](https://erdos.sdslabs.co/tags/probability)

[Problem #100](https://erdos.sdslabs.co/problems/100)

## Quadratic Chaos

Let *m* be an integer such that 1 ≤ *m* ≤ 1000. Find the probability *p* of selecting at random an integer *m* such that the quadratic equation 6*x*2−5*mx*+*m*2 = 0 has at least one integer solution.

Give answer as *p*×1000.

[probability](https://erdos.sdslabs.co/tags/probability)

[Problem #101](https://erdos.sdslabs.co/problems/101)

## Fibonacci Twist

Find 67th term of the sequence whose initial terms are as follows:

0th term: power of 3 in   
1st term: power of 2 in   
2nd term: power of 3 in   
3rd term: power of 2 in   
4th term: power of 2 in   
5th term: 16  
6th term: 19

[implementation](https://erdos.sdslabs.co/tags/implementation)

[Problem #102](https://erdos.sdslabs.co/problems/102)

## Chinese Whispers

Consider a group of 5011 friends and a particular person in the group (say L). L has a message to spread around. Define a “whisper” as an instance where a friend passes the message to another friend. Considering all friends to be distinct, L is interested in finding out the number of sequences of 999983 “whispers” after which he will eventually get the message back. Calculate the answer modulo 1000000007.

**Note**:

After a whisper, if A passed the message to B, then only B can whisper to others since only he has the message. Others can’t.

During the sequence of whispers, there can be a point in time where A would get the message after less than 999983 whispers. In that case, he again should pass the message to others in order to complete a total of 999983 whispers

[dp](https://erdos.sdslabs.co/tags/dp)

[Problem #103](https://erdos.sdslabs.co/problems/103)

## Sevens and Threes

Find the sum of all 7 digit numbers which satisfy the following conditions:

1. It contains only digits 3 and 7.

2. The number is divisible by 7.

3. Last digit of number is 3.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [modular](https://erdos.sdslabs.co/tags/modular)

[Problem #104](https://erdos.sdslabs.co/problems/104)

## Dr. Antlove

Dr. Antlove loves ants (obviously) and he cannot stand anything happening to his ants. Dr. Rage wants to play with him a little. So he challenges him with a trick puzzle. He gives Dr. Antlove a regular polygon with 628318531 sides with Queen ant in the middle and gives him a triangular (ant-trap)net that can be tied at any three random vertices of the polygon(any three vertices can be chosen as the vertices of the net at random). But Dr. Antlove is busy with a seminar this weekend. So he orders you to get the ant for him. Before moving on you believe it would be better to calculate the probability of your success. All choices of vertices being equally likely, let the probability that you would be able to catch the ant inside that net be *p*. (All vertices are distinct.)

Give the answer = 

[geometry](https://erdos.sdslabs.co/tags/geometry) [probability](https://erdos.sdslabs.co/tags/probability)

[Problem #105](https://erdos.sdslabs.co/problems/105)

## Vikas and Pizzas

Vikas has currently ordered a pizza from Domino's. Due to many orders, Domino's did not cut the pizza into slices. He was wondering how many maximum pieces can be made of a pizza with n cuts keeping the pizza fixed at its position.

Find the answer when *n* = 65536.

[geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #106](https://erdos.sdslabs.co/problems/106)

## Back Propagate

Let the initial terms of a sequence be {1,1,1,1,2,11,84,676,5477,44407}.

Propagate this sequence backwards to produce 20 new terms. Find the sum of these 20 terms (written in simplest fraction form as *p*/*q*). What is the value of (*p*\**q*) mod (109+7)?

[dp](https://erdos.sdslabs.co/tags/dp)

[Problem #107](https://erdos.sdslabs.co/problems/107)

## Negated Twins

Let *f*(*x*) be a polynomial with integer coefficients such that

*f*(2) = *f*(0) = *f*(1) = *f*(5) = *n* and

*f*(−2) = *f*(−1) = *f*(−5) = −*n* for some positive integer *n*.

Find the smallest possible value of *n*.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #108](https://erdos.sdslabs.co/problems/108)

## Divisor Game

Consider a two player game. There are *N* balls marked 1 to *N*. A move consists of removing a ball n and all the remaining balls which are divisors of *n* (including 1). The players alternate the moves. The one who takes the last ball wins the game. Let us assume that both players play optimally. Find the probability that the player who starts the game wins it, given that *N* will be a random integer between 1 and ∞. Let this probability be *x*. Give your answer as *x*×1000000000000.

[games](https://erdos.sdslabs.co/tags/games)

[Problem #109](https://erdos.sdslabs.co/problems/109)

## Extension Conundrum

We have a triangle with side lengths *a* = 345678, *b* = 456784 and *c* = 567890 with vertices named *A*, *B* and *C*, and *I* denote the incentre of circle. Line segment *BI* is extended to meet opposite side of triangle i.e. *AC* at *K*. Find length of line segment *IK*.

Note : *a* is side opposite to vertex *A*, *b* is opposite to vertex *B* and *c* is opposite to vertex *C*.

[geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #110](https://erdos.sdslabs.co/problems/110)

## L's Birthday

L was celebrating his birthday. His mom made a triangular cake as per L’s request as he found that round cakes were too mainstream. After the candles were blown, L’s friends (who were 9973 in number) decided that they wanted triangular cake pieces. As L’s mom is fair towards his friends, she has the task to divide the cake into 9974 triangles of equal volume. Like L, even his mom likes a good challenge. So she decided to cut the cake in the following way:

She would select a point *P* on the triangular surface and from *P* she would trace 9974 rays which will intersect the sides of the triangular surface and cut through the rays resulting in 9974 triangular cake pieces of equal volume. But L pointed out that this type of partitioning is not possible for any interior point on the surface. So she is interested in finding out the number of interior points (*P*) wherein such equal partitioning of the cake is possible.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #111](https://erdos.sdslabs.co/problems/111)

## Rectangle has Children

A rectangle 'A' is said to be the child of rectangle 'B' if following 3 conditions are satisfied:

a. 'A' can be completely fit inside 'B' without A's sides touching B's sides.

b. At Least one side of 'A' should be greater (in length) than both the sides of 'B'

c. A’s and B’s sides are positive integers.

A rectangle with sides of length 22543 units and 22541 units has how many children?

(Note : A square is also a rectangle with equal sides)

(Note : A’s (Child) sides need not be parallel to B’s sides when A is fit inside B).

[geometry](https://erdos.sdslabs.co/tags/geometry) [implementation](https://erdos.sdslabs.co/tags/implementation)

[Problem #112](https://erdos.sdslabs.co/problems/112)

## Rooted Sums

Find the answer to the following summation:



Let the answer be *x*. Submit the answer as

[Problem #113](https://erdos.sdslabs.co/problems/113)

## Monica's Candy Fever

We all know how much Monica loved candies in her childhood. And, her excessive competitiveness is no big secret! There have been various incidents where the Gellars had brought home some candies (say *n*). Monica always wanted to have more candies than Ross. Now, the Gellars actually gave the candies randomly to both of them. In spite of the randomness, Monica got more candies than Ross every single time! Now, we want to calculate the probability that Monica had more candies than Ross at every instant that the candies were being distributed. Let the probability of that be *F*(*n*). Calculate. Submit.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics) [probability](https://erdos.sdslabs.co/tags/probability)

[Problem #114](https://erdos.sdslabs.co/problems/114)

## Revenge with Derangement

Suppose that there are *N* persons who are numbered 1,2,...,*N*. Let there be *N* hats, also numbered 1,2,...,*N*. We have to find the number of ways in which no one gets the hat having same number as his/her number.

Let the number of ways to accomplish the above task be *D*(*N*) . You need to enter the value of *D*(*N*) mod *P*.

Take *N* = 49770435560715869 and *P* = 223092870.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics) [chinese remainder theorem](https://erdos.sdslabs.co/tags/chinese%20remainder%20theorem)

[Problem #115](https://erdos.sdslabs.co/problems/115)

## 42: The Answer to Everything?

Represent 42 as the sum of *N* positive real numbers *X*1 , *X*2 , … *XN* where *N* is an integer, such that the product, *P* = *X*1*X*2…*XN* is maximised. Find  where  is greatest integer function.

[calculus](https://erdos.sdslabs.co/tags/calculus)

[Problem #116](https://erdos.sdslabs.co/problems/116)

## Funny Factorial

In a right angled triangle *ABC* right angled at *B*, equations of median *AD* and *CF* are *y* = *x* + 1 and *y* = 2*x* + 4 respectively . Given *AC* is 60 units find the last five non zero digit of (*X*)! where *X* is the area of triangle *ABC*.

[geometry](https://erdos.sdslabs.co/tags/geometry) [brute force](https://erdos.sdslabs.co/tags/brute%20force)

[Problem #117](https://erdos.sdslabs.co/problems/117)

## Expectation Frenzy

Suppose an M-faced fair dice is tossed *N* times. Whenever the dice is tossed, each face appears with probability 1/*M*. After *N* throws of the dice, let the expected value of minimum number obtained on the dice be E. Enter the value of  where  is greatest integer function.

Take *M*=100 and *N*=20.

[probability](https://erdos.sdslabs.co/tags/probability)

[Problem #118](https://erdos.sdslabs.co/problems/118)

## Analyzing Complexity

Problems with which we often deals in programming requires us to approximate number of iterations that we are going to perform in loops.

Given below is a simple pseudo code for which you need to tell the number of iteration performed in the given nested list :

for ( int x1 = 1 ; x1 <= n ; x1++ )

for ( int x2 = x1 ; x2 <= n ; x2++ )

for ( int x3 = x2 ; x3 <= n ; x3++ )

……

……

……

for ( int xm = x(m-1) ; xm <= n ; xm++ )

it++ ;

Take initial value of it as 0 and value of m and n to be 25 and 26 respectively.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #119](https://erdos.sdslabs.co/problems/119)

## Minimum Cubes

We define *f*(*x*) = minimum number of positive perfect cubes that sum up to *x*.

For example,

*f*(2)=2(2=13+13)

*f*(9)=2(9=13+23)

*f*(17)=3(17=13+23+23)

Find .

[dp](https://erdos.sdslabs.co/tags/dp)

[Problem #120](https://erdos.sdslabs.co/problems/120)

## Balance the Weight

You are given a beam balance and *N* objects where *i*th object weighs 2*i*−1 , 0 < *i* <= *N*. *F*(*N*) denotes the no. of ways of placing these objects(one by one) on balance such that the left side is always heavy (after every placement). Find the value of *F*(100) and give the answer modulo 109+7.

[implementation](https://erdos.sdslabs.co/tags/implementation) [constructive algorithms](https://erdos.sdslabs.co/tags/constructive%20algorithms)

[Problem #121](https://erdos.sdslabs.co/problems/121)

## The Game of Fibonacci and Powers of Two

You are given a pile of stones. Two people play this game turn by turn. In any turn, a player can remove a number of stones from the pile, say *X*, such that *X* can be either a non zero Fibonacci number or a power of 2.

The person that empties the pile wins the game. Both the persons play optimally, i.e. they try to make the best possible move that will help them win. If the number of stones in the pile varies between 1 and 106, in how many cases will the first player lose?

[dp](https://erdos.sdslabs.co/tags/dp) [games](https://erdos.sdslabs.co/tags/games)

[Problem #122](https://erdos.sdslabs.co/problems/122)

## Never Ending Fraction

Given that



for *n* > 0 (*n* is an integer) where

*P*0 = 0 and

*Q*0 = 1.

Calculate (*P*1000\**Q*1000) mod (1000000007)

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [recurrence](https://erdos.sdslabs.co/tags/recurrence)

[Problem #123](https://erdos.sdslabs.co/problems/123)

## Recurring Roots

Let  for *x* >= 2 and *x* < *y* where *x* and *y* are integers.

Also, let *g*(*x*) = *T* where *T* is the smallest integer such that *x* < *T*.

Let *h*(*x*) = 2*x* mod 1000000007

Find out *h*((*g*(*f*(*g*(*f*(42,111111111111111)),222222222222222))))).

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [induction](https://erdos.sdslabs.co/tags/induction)

[Problem #124](https://erdos.sdslabs.co/problems/124)

## Co-prime judgement

We define *φ*(*n*) as the number of positive integers less than or equal to *n* that are relatively prime to *n*.

Lets define *S*(*n*) = ∑*φ*(*d*) over all the divisors of *n* (i.e. *d* divides *n*).

Also define *F*(*n*)=∑*S*(*x*) where *x* varies from 1 to *n*.

Compute the value of *F*(999999) + F(888888)

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #125](https://erdos.sdslabs.co/problems/125)

## Happy String

You are given *p* *a*'s and *q* *b*'s. You arrange them in the form of a string. If you are able to get a string in which as you move from left to right, the number of *a*'s is strictly greater than *b*, then it is known as a happy string.

Let the number of such happy strings be denoted by *happy*(*p*,*q*), then find *happy*(200,100) \* 201! \* (101!/300!).

[probabilities](https://erdos.sdslabs.co/tags/probabilities)

[Problem #126](https://erdos.sdslabs.co/problems/126)

## Playing with constraints

Let *x* = last 7 non-zero digit of 9999!

Define *F*(*n*,*k*) = Sum of *k*th powers of all divisors of *n*, so for example *F*(6,2)=12+22+32+62=50

Define further *G*(*a*,*b*,*k*) as: Sum of *F*(*j*,*k*) where *j* varies from *a* to *b* both inclusive

You need to enter the value of *G*(1,*x*\**x*,2) modulo (109+7)

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #127](https://erdos.sdslabs.co/problems/127)

## Decamping Twice

Let *S* be a set where *S* = {1,2,3,4,5…...4444444444} and *P* be a subset of *S* such that *x*  *P* but 2*x*  *P*. Let |*T*| be the total number of elements in the set *T*. Find out maximum |*P*| of all the possible subsets *P*.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #128](https://erdos.sdslabs.co/problems/128)

## Fibonacci Fun

Given:



where *ai* = *i*th fibonacci number, e is the Euler’s number and *xi* is a real variable (i.e. *a*1 = 1, *a*2 = 1, *a*3 = 2 ..)

Let minimum value of:  be *Z* at *xi* = *yi* where all *xi* satisfy the above condition.

Let 

Find the greatest integer ≤ 100*k*

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [fibonacci](https://erdos.sdslabs.co/tags/fibonacci)

[Problem #129](https://erdos.sdslabs.co/problems/129)

## Fragger and his sequence

Fibonacci sequence is defined as follow: *F*1 = 1, *F*2 = 2, *Fi* = *Fi*−1 + *Fi*−2 (*i* > 2)

Every natural number *X* can be represented in Fibonacci system such that *X* is sum of one or more distinct Fibonacci numbers in such a way that the sum does not include any two consecutive Fibonacci numbers.

Let  where  and *Ak* = 1

We will represent *X* in Fibonacci system as : *AkAk*−1*Ak*−2………..*A*1 Example 1 = (1)*F*, 2 = (10)*F*, 3 = (100)*F*, 4 = (101)*F*

If we write representation of all natural numbers in Fibonacci system consecutively we will obtain a new sequence (say fragger sequence) which will look like this : 1,1,0,1,0,0,1,0,1…….

You need to count the number of times 1 appears in the first 1015 terms of fragger sequence.

[fibonacci](https://erdos.sdslabs.co/tags/fibonacci) [dp](https://erdos.sdslabs.co/tags/dp)

[Problem #130](https://erdos.sdslabs.co/problems/130)

## The Start

Let , where *ak* = (*k*\*(*k*+2))−1 . Let *Sn* = (*p*/*q*), where *p* and *q* are positive integers and gcd(*p*,*q*) = 1. Find the value of *p*\**q* for *n* = 112358.

[series](https://erdos.sdslabs.co/tags/series) [summation](https://erdos.sdslabs.co/tags/summation)

[Problem #131](https://erdos.sdslabs.co/problems/131)

## Crazy sum

Let *f*(*n*) = ∑*d*|*n* *μ*(*d*)*h*(*n*/*d*) where *h*(*x*) = Sum of divisors of *x*

*g*(*n*) = ∑*d*|*n* *μ*(*d*)*f*(*n*/*d*)

Find  modulo 264

Note: here *μ*(*n*) is Mobius Function.

[series](https://erdos.sdslabs.co/tags/series) [summation](https://erdos.sdslabs.co/tags/summation)

[Problem #132](https://erdos.sdslabs.co/problems/132)

## Functions

For a complex number *z*, given a function 

Let *pj* be the *j*-th prime number 

Let 

Find the value of , where *k* = 354216846978542365.

[series](https://erdos.sdslabs.co/tags/series) [functions](https://erdos.sdslabs.co/tags/functions)

[Problem #133](https://erdos.sdslabs.co/problems/133)

## The drunk boyfriend

In a single dimension world, a girl is standing at the point *x* = 0. Her boyfriend is standing at some point *x* = *x*0. He is drunk. So, he either takes a step towards her girlfriend or a step away, with equal probability. But he can’t go beyond *x* = *n*, because of a wall placed there, So whenever he reaches *x* = *n*, he has to go back to *x* = (*n*−1). Let the expected number of steps for him to reach his girlfriend be *F*(*x*0,*n*) where x0 is his starting point.

Find the value of  for *N* = 107

[probability](https://erdos.sdslabs.co/tags/probability)

[Problem #134](https://erdos.sdslabs.co/problems/134)

## Triangles Counting

Find the sum of all positive integers up to 108 which can be expressed as a hypotenuse of a right angled triangle where other two sides are also positive integer.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #135](https://erdos.sdslabs.co/problems/135)

## Polynomial Expansion

We wish to generate 1000000 pseudo-random numbers *sk* in the range ±219, using a type of random number generator (known as a Linear Congruential Generator) as follows:

t := 0

for k = 1 up to k = 1000000:

t := (615949\*t + 797807) modulo 2^20

sk := t−219

Thus: *s*1 = 273519, *s*2 = −153582, *s*3 = 450905 etc.

We need to find a polynomial *P*(*x*) of lowest possible degree such that *P*(*i*) = *si* for all integers *i* <= 1000000

Enter the value of (*P*(1)+....*P*(1000100)) modulo (1000000007)

[polynomial](https://erdos.sdslabs.co/tags/polynomial) [binomial](https://erdos.sdslabs.co/tags/binomial)

[Problem #136](https://erdos.sdslabs.co/problems/136)

## Equate It

Let *a*, *b*, *c* be positive integers such that *a* ≠ *b* ≠ *c* and *a* divides *b*69, *b* divides *c*69 and *c* divides *a*69. Find min *m* such that that *abc* divides (*a*+*b*+*c*)*m* for any *a*, *b*, *c* satisfying the above condition.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #137](https://erdos.sdslabs.co/problems/137)

## Harry Potter and Horcrux

In a two dimensional map Harry initially is standing at some point denoted by character ‘H’. Also there is a horcrux at some point of map denoted by character ‘X’. In order to protect that horcrux You-Know-Who has appointed several Death Eaters at certain points of map denoted by character ‘D’.

Harry need to find the horcrux but he is not knowing the exact position of horcrux and hence he will walk in any of the four direction (left, right, top, bottom) with equal probability from his position as long as he stays in map and not go to any place where Death Eaters reside. Points on which Harry can walk will be denoted by ‘W’ in map.

Harry is determined to find the horcrux and he will not stop until he finds it. You need to find expected number of steps Harry will take to find the horcrux.

There are 20 maps in “maps.txt”. For each map first its dimensions are given *m*,*n* which indicates map size *m*×*n* .After which map is given in described format. NOTE: There always exist a path between Harry and horcrux for map given in input.

Let the sum of expected value for all map be P. Enter the value of floor(*P*\*103). Link to [**maps.txt**](https://erdos.sdslabs.co/files/problems/137.txt)

[probability](https://erdos.sdslabs.co/tags/probability) [graph](https://erdos.sdslabs.co/tags/graph)

[Problem #138](https://erdos.sdslabs.co/problems/138)

## Mul Me

Let the number of ordered quadruples satisfying this equation be *f*(*n*)

*a*\**b*\**c*\**d* <= *n*

*f*(1) = 1

*f*(2) = 5

Find *f*(1012)

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #139](https://erdos.sdslabs.co/problems/139)

## Sum Me

Let *F*(*n*) = sum of all divisors of *n*.

Find the sum of all *n* such that *F*(*n*) = 2\**n* and 1 <= *n* <= 5\*1035

Report your answer modulo 109+7.

[number theory](https://erdos.sdslabs.co/tags/number%20theory)

[Problem #140](https://erdos.sdslabs.co/problems/140)

## Bored with GCD

Define 

Also 

Find the value of 

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [gcd](https://erdos.sdslabs.co/tags/gcd)

[Problem #141](https://erdos.sdslabs.co/problems/141)

## Complex Summation

An nth root of unity, where *n* is a positive integer (i.e. *n* = 1, 2, 3, …), is a number *z* satisfying the equation:

*zn* = 1

An *n*th root of unity is primitive if it is not a kth root of unity for some smaller *k*:

*zk* ≠ 1 (*k* = 1,2,3,...,*n*−1)

Let *S*(*n*) be the sum of all the primitive *n*th roots of unity.

Define 

Enter the value of *F*(1011,103) mod 1000000007.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [algebra](https://erdos.sdslabs.co/tags/algebra) [complex numbers](https://erdos.sdslabs.co/tags/complex%20numbers)

[Problem #142](https://erdos.sdslabs.co/problems/142)

## Inequality Marathon

Let *S*=*X*1,*X*2,*X*3…...*Xk* where 0<=*Xi*<=1 for 1<=*i*<=*k* and .

Also 0<=*P*(*x*)<=1 for all *x*∈*S*. Given that .

Let us say *T* = Max ()

Also,  (log with base 2).

Given that Max(*F*(*x*))=13.

Find (*T*!) mod 1000000007

[probability](https://erdos.sdslabs.co/tags/probability) [inequality](https://erdos.sdslabs.co/tags/inequality)

[Problem #143](https://erdos.sdslabs.co/problems/143)

## Exponential Fibonacci

Let *Fn* be the *n*th fibonacci number where *F*0=0 and *F*1=1.

Also let  and .

If *Fx*=gcd(*Fa*,*Fb*) where *x* can be represented as 27*y*.

If (*Fm*)3 − (*Fn*)3 = *Fy* − (*Fy*/3)3

Find the value of (m\*n) mod 1000000007.

[fibonacci](https://erdos.sdslabs.co/tags/fibonacci) [matrix exponentiation](https://erdos.sdslabs.co/tags/matrix%20exponentiation)

[Problem #144](https://erdos.sdslabs.co/problems/144)

## Circular paradigm

Let the number of arrangements of 3*n* identical Type A balls and 3 identical Type B balls in a circle be *F*(*n*). Find *F*(100000)\**F*(100001).

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #145](https://erdos.sdslabs.co/problems/145)

## Vasu And Houses

We have a total of *n*-1 persons (*P*1,*P*2,...*Pn*−1) and *n* houses (*H*1,*H*2,*Hn*).

Find the number of ways for *n*=6 such that each person visits only 1 house and the following conditions are satisfied:

1. Each person visits a different house

2. Person *Pi* can’t visit House *Hi*

3. *P*1 can’t visit House *Hn*

[derangements](https://erdos.sdslabs.co/tags/derangements)

[Problem #146](https://erdos.sdslabs.co/problems/146)

## A Very Easy Sum

A number is called special if when prime factorized as , then *ai*<=2 for all 1<=*i*<=*k*.

Let *S*(*N*) be the sum of all special numbers from 1 to *N*.

Given *S*(10)=47 and *S*(104)=41586160

Enter *S*(123456789123456789) modulo 109+7.

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [summations](https://erdos.sdslabs.co/tags/summations)

[Problem #147](https://erdos.sdslabs.co/problems/147)

## Divisor Sum

Define *F*(*n*,0)=1

, where *d*|*n* means *d* is a divisor of *n*.

Let 

Given *S*(9876,234) mod 1000000007 = 208863976

Enter the value of *S*(98765432,2345678) mod 1000000007

[number theory](https://erdos.sdslabs.co/tags/number%20theory) [divisors](https://erdos.sdslabs.co/tags/divisors) [summations](https://erdos.sdslabs.co/tags/summations)

[Problem #148](https://erdos.sdslabs.co/problems/148)

## Levels in Tree

Consider a tree with *n* nodes rooted at node 1. We define parent[*i*] as the parent of *i*th node. For each 2<=*i*<=*n* , parent[*i*] can assume any value from 1 to *i*−1 with equal probability. Let *F*(*n*) the expected value of the sum of levels of all nodes. 1st node is at level 1 and for each 2<=*i*<=*n*, if node *i* has level *x*, parent[*i*] has level *x*−1.

Given *F*(10)=29.28968

Enter your answer as the greatest integer less than or equal to *F*(12345678) .

[probabilities](https://erdos.sdslabs.co/tags/probabilities)

[Problem #149](https://erdos.sdslabs.co/problems/149)

## Fibonacci Sum

Define: *F*(0)=0

*F*(1)=1

*F*(*n*)=*F*(*n*−1)+*F*(*n*−2), *n*>=2

Define mod 1000000009

Given *S*(1012,100)=878943097

Enter the value of 

[fibonacci](https://erdos.sdslabs.co/tags/fibonacci) [modular roots](https://erdos.sdslabs.co/tags/modular%20roots)

[Problem #150](https://erdos.sdslabs.co/problems/150)

## Fun with Expectation

Consider an array of *n* numbers where each element can be any non negative *x* bit number (0 to 2x−1) with equal probability. Let *F*(*n*,*x*) be the expected value of the sum of bitwise xor of all possible subsequences of the array.

Eg. Consider the array 1,2,3.

Sum of xor of all possible subsequences of this array = 1 + 2 + 3 + 1^2 + 1^3 + 2^3 + 1^2^3 = 1 + 2 + 3 + 2 + 1 + 3 + 0 = 12.

Note: ^ is the bitwise xor operation here.

*F*(2,2)=4.5

Enter your answer as floor(*F*(29,30)+*F*(30,29)).

[probabilities](https://erdos.sdslabs.co/tags/probabilities) [bits](https://erdos.sdslabs.co/tags/bits)

[Problem #151](https://erdos.sdslabs.co/problems/151)

## The Pebble Game

Given a Directed Acyclic Graph ([DAG](https://en.wikipedia.org/wiki/Directed_acyclic_graph)) , at a given instant of time we can do one of the following two operations:

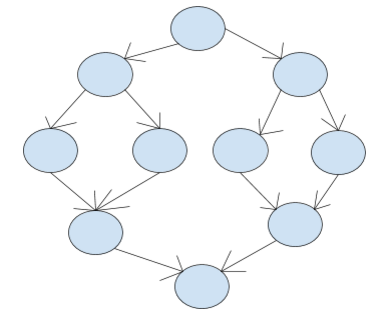
1) Place pebble on a node,if all its immediate ancestors have a pebble

2) Remove pebble from a node.

Initially, there are no pebbles on any node of the DAG.

Our goal is to minimize the maximum number of pebbles over time such that finally, pebbles are on all leaf nodes (nodes with no outgoing edges) . Assume all DAGs of the form: 2 equal height full binary trees, one kept inverted. The leaves of each binary tree are at the same level.

Eg.: This is a DAG made to resemble 2 binary trees of height 2.



Say *F*(*n*)= Answer for a DAG similar to 2 binary trees of height *n*.

Find

[graphs](https://erdos.sdslabs.co/tags/graphs)

[Problem #152](https://erdos.sdslabs.co/problems/152)

## Modular Test

Let *Fp*(*x*) = maximum *k* such that *pk* divides *x*!

Let *Gp*(*x*)=*pFp*(*x*)

Let 

Let 

Enter the value of *S*(105)

[chinese remainder theorem](https://erdos.sdslabs.co/tags/chinese%20remainder%20theorem) [factorial](https://erdos.sdslabs.co/tags/factorial)

[Problem #153](https://erdos.sdslabs.co/problems/153)

## Costly Coins

Akhil has 100000000 coins in his FlipCart. He spreads them on a table. Initially all of them are facing head. Daga selects any 34117 coins at random and inverts all of them. Daga repeats this process 1000 times.

What is the expected number of head after the process?

Submit the integer part of the expected number (ignoring the part after decimal point).

[expectation](https://erdos.sdslabs.co/tags/expectation)

[Problem #154](https://erdos.sdslabs.co/problems/154)

## Vikas and Cows

Vikas has a rectangular farm of dimensions a\*b in 'Amazon' forest. He also has 4 cows. The 4 cows are very aggressive. So he ties his cows to the 4 corners of the farm through ropes. The length of ropes are r1, r2, r3, r4. He wants to maximise the grazing area. But, as the cows are aggressive, he does not want the cows to fight.

*F*(*a*,*b*)= Maximum area of the farm that can be grazed by the cows



Output 

[geometry](https://erdos.sdslabs.co/tags/geometry)

[Problem #155](https://erdos.sdslabs.co/problems/155)

## Irreconcilable Differences

Saurv4u and Daenerys were a loving couple. But due to 'Irreconcilable Differences', the couple is thinking of 'breaking' up.

To measure the depth of the differences *D*, Saurv4u has shaded the inner region of the rectangles (The sides of the rectangle are parallel to the Cartesian axes and the center of rectangle is origin) such that the perimeter of rectangle is less than 4\**a* , while Daenerys has shaded (on the same plane) the inner region of all the rectangles (The sides of the rectangle are parallel to the Cartesian axes and the center of rectangle is origin) such that the area of rectangle is less than 3\*a\*a/4.

The measure of the depth of differences *D* is the common area bounded by the two.

Given the value of *a* = 1000, find the value of 

 means the greatest integer <= *x*

[geometry](https://erdos.sdslabs.co/tags/geometry)

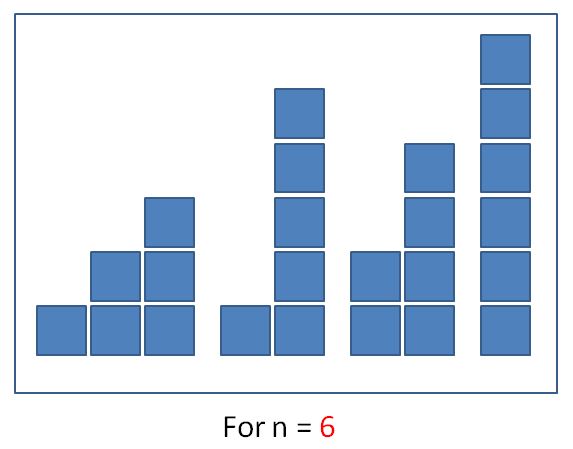
[Problem #156](https://erdos.sdslabs.co/problems/156)

## The Next Big Tower

Princi is playing 'Make Towers with Blocks'. She wants to make towers and then jump from one tower to the next.

The rules of the game are: She has *N* blocks. She can make any number of towers with them but the heights of the towers must be in a strictly increasing order i.e. height of any two towers must not be equal (so she can jump higher and higher).

Now she wants to find the number of ways in which she can make towers like this with *N* = 196 blocks (the different ways for *N* = 6 are shown in the image). Since, she is busy doing her work, you have to find the answer for her.



[dp](https://erdos.sdslabs.co/tags/dp)

[Problem #157](https://erdos.sdslabs.co/problems/157)

## For the love of tomatoes

Mishra loves to eat tomatoes. He likes tomatoes so much that he shares them with no one (not even, well, no one). Mishra likes to store his tomatoes safely. He puts all his tomatoes in boxes and puts all boxes in a 3D Cartesian space on the coordinates (*i*,*j*,*k*) such that 1<=*i*<=*N*,1<=*j*<=*N* and 1<=*k*<=*N* So there are a total of *N*3 boxes.

Now, adkroxx wants to steal his tomatoes. He has the following information:

* Number of tomatoes in each box is different.
* Number of tomatoes in any box *Aijk* is 1<=*Aijk*<=*N*3
* The number of tomatoes in each row along positive x axis is strictly increasing.
* The number of tomatoes in each row along positive y axis is strictly increasing.
* The number of tomatoes in each row along positive z axis is strictly increasing. Now, before stealing the tomatoes, adkroxx defines ADK*i* as the product of all possible values of *Aiii*

*P*(*N*) is given by:



Find *P*(*N*) for *N* = 216. Give the answer modulo 109+7 .

[brute force](https://erdos.sdslabs.co/tags/brute%20force)

[Problem #158](https://erdos.sdslabs.co/problems/158)

## Best Hacker in the World

Foxtrot and Vampire decided to play a game to decide who is a better hacker. They have *n* tiles in a line out of which *m* are white rest all are black. Their task is to change all the black tiles with white by following a simple procedure. They can change a black tile with white only if there is atleast one white tile adjacent to that black tile. Now they have *n* = 74 and *m* = 13 and the 13 positions (indexed 1) of white tiles are 6,14,19,20,21,24,30,43,58,61,69,70,73

They want to find the total number of ways in which it can be done. Help Vampire find the answer as he cannot come out in daytime.

Report your answer modulo 109+7.

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #159](https://erdos.sdslabs.co/problems/159)

## Revenge of The Fox

After losing to Vampire, Foxtrot wants to take revenge.

Vampire has 30 piles of coins, each contains *N* number of coins. Every gold coin weighs 10 grams, while counterfeit coin weighs 9 grams. Some of the piles contain all counterfeit coins. He has a digital scale capable of accurately weighing any number of coins. He knows that at most 3 of the 30 piles are counterfeit. He needs to find the minimum value of *N* so that, with just one measurement, he can guarantee identifying which (if any) piles are counterfeit. Vampire is busy in some work and says if Foxtrot can solve this for him, he will declare Foxtrot as the best hacker.

Find the answer for Foxtrot.

[Problem #160](https://erdos.sdslabs.co/problems/160)

## Such Sum Wow

Vaibhav is participating in MCA PCIC - largest international Math competition where he gets this problem:

Given *N* equations of the form:

, *i* varies from 1 to *N*,

where *ai* = *bi* = *i*th Fibonacci number and *ci* = (*i*+2)th Fibonacci number.

Let  for all the equations.



Submit *h*(*N*) mod (109+7) for *N* = 987654321342198766.

Note: Fibonacci series:

Fib[0] = 0, Fib[1] = 1, Fib[i] = Fib[i−1] + Fib[i−2]

Now Vaibhav doesn't like maths, so you have to solve it for him.

[fibonacci](https://erdos.sdslabs.co/tags/fibonacci)

[Problem #161](https://erdos.sdslabs.co/problems/161)

## Binary Play

Consider a set *S*(*N*) such that *S*(*N*) contains all sequences of 0 and 1 of length *N* in which no two 1′s are adjacent. For example:

*S*(3)=(000,001,010,100,101)

Let *A* = No. of elements in *S*(30)

*B* = Sum of digits of *A*

You have to output no. of 0 appearing in *B*th sequence of *S*(30) when arranged lexographically.

[fibonacci](https://erdos.sdslabs.co/tags/fibonacci) [dp](https://erdos.sdslabs.co/tags/dp)

[Problem #162](https://erdos.sdslabs.co/problems/162)

## One Last Game

During a game of Mafia, after Verma is killed by Mafia in the first round, he starts getting bored and keeps disturbing others in the game. This irritates everyone else and to keep the game interesting, Akhil asks Adarsh to keep Verma occupied in something else.

So Adarsh gives him a 1\**N* matrix which has *N* cells. Also, he gives him *M* colours numbered from 1 to *M* . Now, Verma can choose any submatrix with even number of cells from the matrix and colour it with one of the *M* different colours. He can colour as many times as he wants . If Verma tries to recolour any cell which is already coloured, the cell gets coloured in the last colour.

Adarsh asks Verma to make as many distinct matrices that he can make such that every cell is coloured. Each matrix is different from other if atleast one of the cell has a different colour.

Find the number of matrices Verma can make and submit the answer modulo 1000000007

Take *N* = 99999999999999 and *M* = 999999999

[combinatorics](https://erdos.sdslabs.co/tags/combinatorics)

[Problem #163](https://erdos.sdslabs.co/problems/163)

## Bored with Shinigami

Ryuk is bored with the Shinigami world and goes to the human world to find something interesting. He is fascinated with the GCD function and fibonacci numbers and starts playing with them.

Fibonacci numbers are defined as :

*F*(*n*) = *F*(*n*−1) + *F*(*n*−2) ∀ *n*≥2

with *F*(0) = 0 & *F*(1) = 1.

Ryuk wants you to find the value of gcd(*F*(1012185−172185), *F*(1014807−174807)) mod 1000000007.

[Problem #164](https://erdos.sdslabs.co/problems/164)

## Kill the remaining Chinese

Kira has killed all criminals in Japan and has now started killing Chinese criminals. He kills *Z* criminals every week Where *X* = 100! and *X*9449771607341027425  *Y* mod 9449771616229914661

*Z* = *Y* mod 1000000008.

As a supporter of Kira, help him by finding *Z*.

[Problem #165](https://erdos.sdslabs.co/problems/165)

## L's Successor

L is fighting Kira which can be dangerous as Kira has the Death Note. Watari has to decide a successor for L in case L dies. Watari gives a point (*x*,*y*,*z*) in cartesian plane to Mello and Near and they have to play a game such that they take turns. In one turn, the player can change one of the coordinates (say *w*) to[*w*/2],[*w*/3],[*w*/5].(*w* > 0) So (8,9,10) can be reduced to (4,9,10) or (2,9,10) or (1,9,10) or (8,9,3) and so on. The person who changes the point to origin wins the game. Watari wants Near to win but he forgot the z coordinate so he randomly selects z between 0 and 12345 (both inclusive). So the point is *L*(2^{60}, 2^{61}, *z*), where *z* is between 0 and 12345 (both inclusive). Given that Near starts play calculate the probability that Near will win the game if both players play optimally.

If the answer is of the form *u*/*v* where *u* and *v* are coprime you have to input *u*+*v* as the answer.

[Problem #166](https://erdos.sdslabs.co/problems/166)

## Apples for Ryuk

Light Yagami has to buy apples for Ryuk without attracting any unwanted attention towards himself. Interestingly, the number of apples he buys everyday is always a Fermat Number. A Fermat number is a number of the form . *G*(*N*) = sum of digits of *N*th Fermat Number modulo 9 Find the sum of *G*(*i*) for all *i* between 1 and 999999999999 (both inclusive).

[Problem #167](https://erdos.sdslabs.co/problems/167)

## The Perfectionist Yagami

L gives Light the following challenge and claims that if he is unable to solve it, he is Kira. Help Light deceive L by solving the challenge. A 3-perfect number is defined as a number whose sum of divisors equals thrice that number.you have to fiind the sum of all 3-perfect numbers of the form *n* = 2k3*p* that are less than 109, where *p* is an odd prime number and *k* is positive Integer. Give the answer modulo 109+7.

[Problem #168](https://erdos.sdslabs.co/problems/168)

## L's Ideology

L is sure that Light is kira and Misa is second Kira . He randomly selects two permutation of 1 to *N* and store it in *A*[0],*A*[1],...*A*[N−1] and *B*[0],*B*[1],...*B*[N−1]. All permutations are equally probable . Now he randomly selects a integer *X*, 0 <= *X* < *N* , and shifts permutation *B* to left by *X*.

For Example - [2,3,1,4,5] be a permutation , shifting it left by 2 will result [1,4,5,2,3].

He defines another sequence

*g*[*i*] = (*A*[*i*]\*1) mod *B*[*i*] + (A[*i*]\*2) mod *B*[*i*] + (*A*[*i*]\*3) mod *B*[*i*]......(*A*[*i*]\**B*[*i*]) mod *B*[*i*] .

Find expected value of *g*[0]+*g*[1]+........+*g*[*N*−1] for *N* = 1111.

Answer greatest integer of expected value.

[Problem #169](https://erdos.sdslabs.co/problems/169)

## Attendance and Probability

As we all know adkroxx is a great programmer of our institute. But due to programming he started missing a lot of classes. Now the institute decides to offer him cash reward for good attendance. If he is absent for 4 consecutive days or late on more than one occasion they will forfeit his prize. During an n-day period a ternary string is formed for each day consisting of *L*'s (late), *O*'s (on time), and *A*'s (absent).

Adk being a smart kid tries to find out what is the total number of prize string that exists. Although there are eighty-one ternary strings for a 4-day period that can be formed, exactly forty-seven strings would lead to a prize.

Now you have to help adkroxx to find out number of prize strings for *n* = 10000007 and report the answer modulo 109+7.

[Problem #170](https://erdos.sdslabs.co/problems/170)

## Magical Distance

Consider all points with integral positive coordinate (*x*,*y*) which lies on the curve

|*x*2 − 4*xy* − *y*2| = 1

Let *Pi* be the coordinate of *i*th point when all the points satisfying above equation are sorted in ascending order according to their distance from the origin.

Let *Di* = distance between (0,0) and *Pi*

If 

Enter the value of *S*(1015) mod 1000000009.

[Problem #171](https://erdos.sdslabs.co/problems/171)

## Random Name



Find *F*(12345678) mod 109+7

[Problem #172](https://erdos.sdslabs.co/problems/172)

## Polynomial Expansion 2

Consider 

Consider 

Let *R*(*k*,*x*) be the remainder obtained when *f*(*x*)*k* is divided by *g*(*x*).

Example:



Let *S*(*k*,*x*) be the sum of coefficient of *R*(*k*,*x*).

You need to enter the value of *S*(,*x*) modulo 100086841.

[Problem #173](https://erdos.sdslabs.co/problems/173)

## Permutation mania

Permutation *p* is an ordered set of integers *p*1,*p*2,...,*pn* consisting of *n* distinct positive integers, each of them doesn’t exceed *n*. We will denote the *i*th element of permutation *p* as *pi*. We will call number *n* the size or the length of permutation *p*1,*p*2,...,*pn*.

We will call position *i* (1 ≤ *i* ≤ *n*) in permutation *p*1,*p*2,...,*pn* good, if |*p*[*i*]−*i*| = 1.

Your task is to count the number of permutations of size *n* with exactly *k* good positions.

Give the answer for *n* = 1000 and *k* = 700 modulo 1000000007.

Example: for *n* = 3 and *k* = 2 answer will be 4.

(1,3,2),(3,1,2),(2,1,3),(2,3,1) all have exactly 2 good position.

[Problem #174](https://erdos.sdslabs.co/problems/174)

## Dabba and Dhakan

Dabba loves Maths and his girlfriend Dhakan, so he either spends his day with dhakan or does maths all day. But he hates spending two consecutive days with dhakan (because she is a dhakan). He wants to make his schedule for his summer vacation as a sequence of doing maths or spending day with dhakan.

No of days of his summer vacation can vary from *l* to *r*. You need to count in how many ways Dabba can select *k* different schedule of the same number of days for his summer vacations, whose days can vary from *l* to *r*.

For example if *k* = 2, *l* = 1 and *r* = 2, if we define Maths day as {1} and Dhakan's day as {0}, here are all possible combination: {0}, {1}, {00}, {01}, {10}, {11}. But '00' can not be selected because it has 2 consecutive Dhakan's day in a row. Now, we need to count in how many ways we can select *k* = 2 schedule of the same length in range [1,2]. Here they are: for no. of days = 1 {0,1}; no. of days = 2 {01,10}; {01,11}; {10,11}. so answer for *k* = 2, *l* = 1 and *r* = 2 will be 4.

He wants you to tell him in how many ways can do that, modulo 1000000007 for *k* = 200, *l* = 1 and *r* = 1018.

[Problem #175](https://erdos.sdslabs.co/problems/175)

## The Rocking Problem

Bunty is trying to solve a problem and he is unable to do it so he asks you to solve his problem.

Let *F*(*n*) is the number of subsets of (1,2,3....*n*) that contain no consecutive integers modulo 1000000007.

Now you have to report *G*(*F*(100000007));

*G*(*n*) = number of binary sequences of length *n* that have no consecutive 0′s modulo 1000000007.

[Problem #184](https://erdos.sdslabs.co/problems/184)

## Color problem

Mr. Pink likes summation series and Mr. White likes to take big powers of numbers. In order to satisfy both of them Mr. Brown want you to evaluate the following sum



modulo 109+7 for *n* = 109 and *k* = 106

[Problem #186](https://erdos.sdslabs.co/problems/186)

## Euler and Fibo



where *k*|*x* means *k* divides *x*, Φ(*n*) is Euler totient



*F*(*n*) = *F*(*n*−1) + *F*(*n*−2) for *n* > 1

*F*(0) = 0 and *F*(1) = 1



Find *Z*0(*n*)*Z*1(*n*) mod109+7 for *n* = 108

[Problem #189](https://erdos.sdslabs.co/problems/189)

## Night King and The Army of the Dead

Night king is marching with an army of the dead. The Night King has *N* deads in his army and they are labelled from 1 to *N*. Jon Snow is trying hard to stop Night King to cross the wall and destroy Westeros. Jon figures out that killing a walker leads to the disintegration of some of his associated wights.

If Jon kills the *k*th dead all the dead with a label which divides *k* will be disintegrated. For *N* = 123456789, what is the minimum number of kills required to clear the army?

[Problem #190](https://erdos.sdslabs.co/problems/190)

## Semi Prime Sum

What is the sum of semi-primes up to 107.

Semi Prime is a number of the form *a*\**b* where *a* and *b* are both prime numbers.

[Problem #191](https://erdos.sdslabs.co/problems/191)

## Save Jon Snow

Jon Snow hands Gendry a message, tells him to go to Eastwatch and send a raven to Daenerys to rescue them. Currently, Gendry is at (0,0) and the castle is situated at (*N*,*N*). In order to escape the battlefield, he can only move from (*i*,*j*) to (*i*,*j*+1) or (*i*+1,*j*) or (*i*+1,*j*+1).

Find the number of paths that can be taken by Gendry to reach the castle modulo 109+7 for *N* = 107.

[Problem #192](https://erdos.sdslabs.co/problems/192)

## Colorful Matrix

Consider a 2000\*2000 matrix which is to be filled with 15 colors. Find the number of ways to color the matrix. Two colorings are same if rotating one of them along the axis perpendicular to the plane (in multiples of 90 degrees) gives the other. Give the answers modulo 109+7.

[Problem #193](https://erdos.sdslabs.co/problems/193)

## Bend the knee or Play

Jon has a well-shuffled deck of *M* = 4999 white cards and *N* = 4999 green cards. Each permutation of cards in the deck is equally likely. Dany has set some rules for Jon. Every time Jon flips a white card he gets one coin, otherwise he loses one coin.At any moment (even at the beginning), Jon is allowed to stop playing the game and keep the number of coins that he has.During the game-play the balance of coins that Jon has may be negative. Let *k* be the expected amount of coins Jon will have if Jon plays optimally. Evaluate [*k*\*10000]\*123456.

[x] represents the greatest integer <=*x*.

[Problem #194](https://erdos.sdslabs.co/problems/194)

## Integers on a roll

Let *F*(*a*) = Number of integral points on the equation is *x*2+ *y*2 = *a*.

Find the sum of  for all values 1<=*a*,*d*,*k*<=100 modulo 109+7.

[Problem #195](https://erdos.sdslabs.co/problems/195)

## Flip 'em all

Consider a row of *N* cards all facing up. Now a player flips all the multiples of 1, then 2 and so on till *N*. Find the number of cards facing up if *N* = 12345678987654321.

[Problem #196](https://erdos.sdslabs.co/problems/196)

## Game of Thrones

In game of thrones you either win or you die. Each one of Jon, Dany, Cersei and Euron are ruling one of the four kingdoms . Ruler who gets to rule two kingdoms sits on the iron throne. Dany decides to attack one of the other kingdoms so that she can sit on the iron throne. But there is a catch. There are three dragons distributed among the 4 rulers in any possible way. (Dany herself can have all the three dragons or maybe she won't have any!) All the dragons are alike and there is no difference between them.

If Dany attacks on a kingdom whose ruler has more dragons than her, she loses. The probability that she sits on the throne is of the form *p*/*q* where *p* and *q* are coprimes and *q* is not equal to zero. Submit the ans *pq* modulo 109+7.

[Problem #197](https://erdos.sdslabs.co/problems/197)

## Kill the King

Daenerys has 3 dragons and 9 XORgons (a creature that can breathe any number from the range [0,123456789] ). If multiple XORgons throw numbers to a target at a time then the resulting number will be the XOR of the individual numbers thrown by each XORgon. Surprisingly the night king can be killed by the number 123456789. Help Tyrion to find out how many ways all 9 XORgons can throw number to the night king such that night king can be killed.

To cut the long story short how many unordered 9−tuples (*a*,*b*,*c*,*d*,*e*,*f*,*g*,*h*,*i*) are there such that *a*∧*b*∧*c*∧*d*∧*e*∧*f*∧*g*∧*h*∧*i* = 123456789 and *a*,*b*,*c*,*d*,*e*,*f*,*g*,*h*,*i* are numbers from the range [0,123456789]. Submit the answer modulo 1000000016000000063.

∧ represents the bitwise XOR operation.

[Problem #198](https://erdos.sdslabs.co/problems/198)

## XOR Again

Find the sum of i∧j modulo 109+7 for all integers i and j in [0,1073742824].

∧ represents bitwise XOR operation.